

Laser Spectroscopy of neutron-rich K isotopes



BRIX Fall Day
2/12/2013

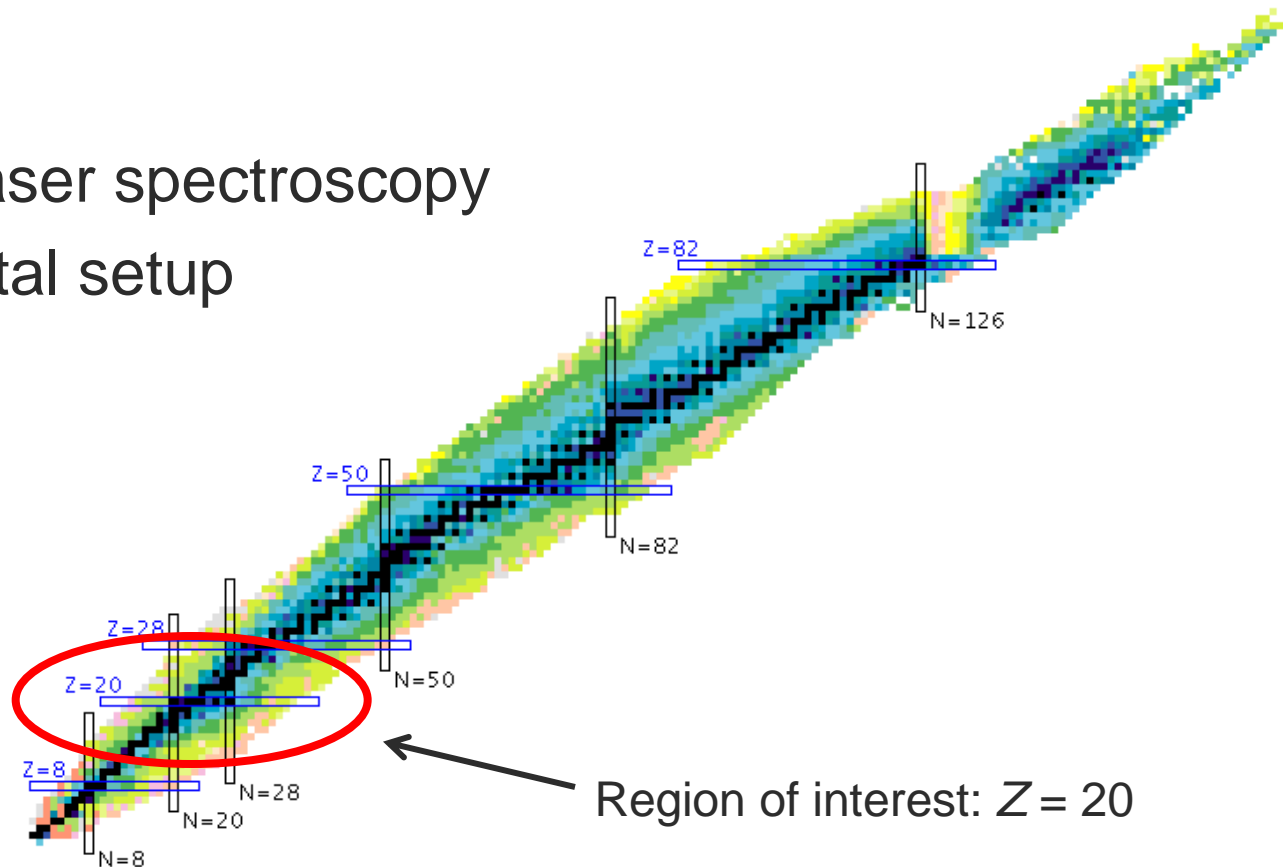
Jasna Papuga



KU LEUVEN

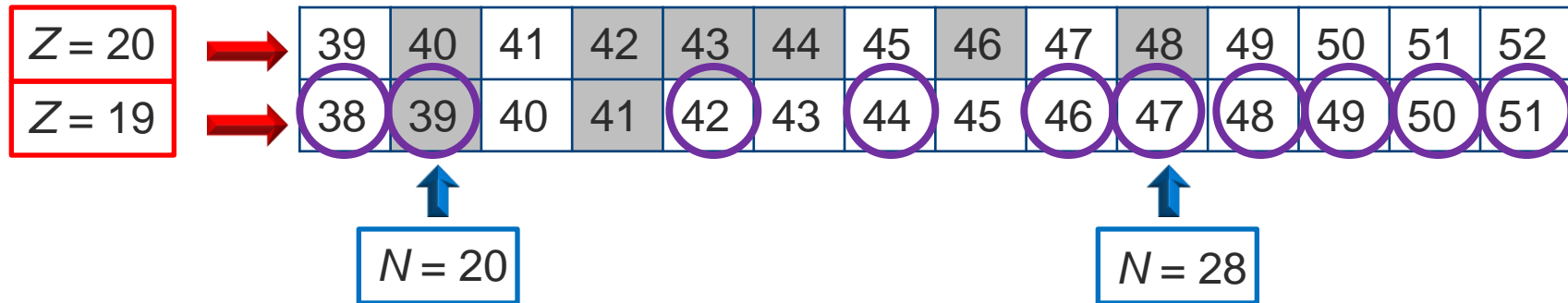
Outline:

- Motivation
- Collinear laser spectroscopy
- Experimental setup
- Results
- Conclusion

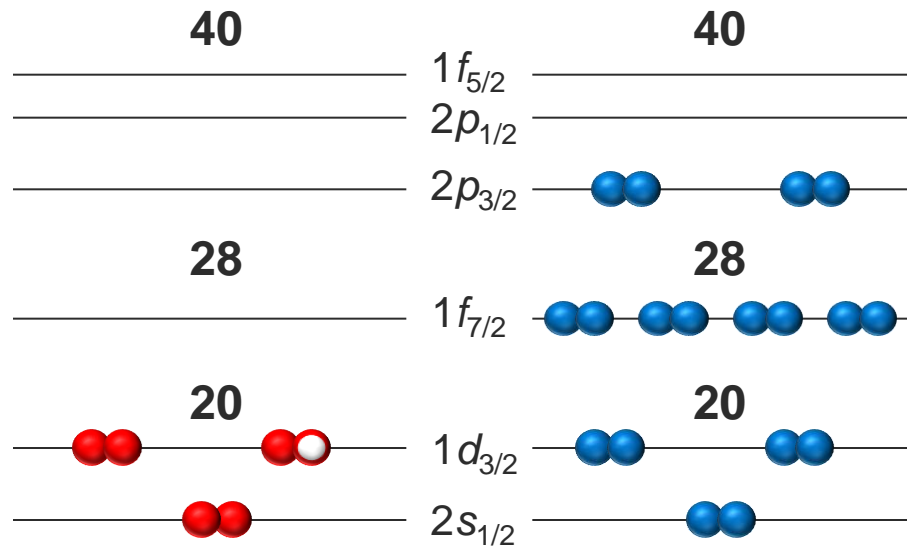


Motivation

Stable isotope
 Experiment



Proton orbits
(π)

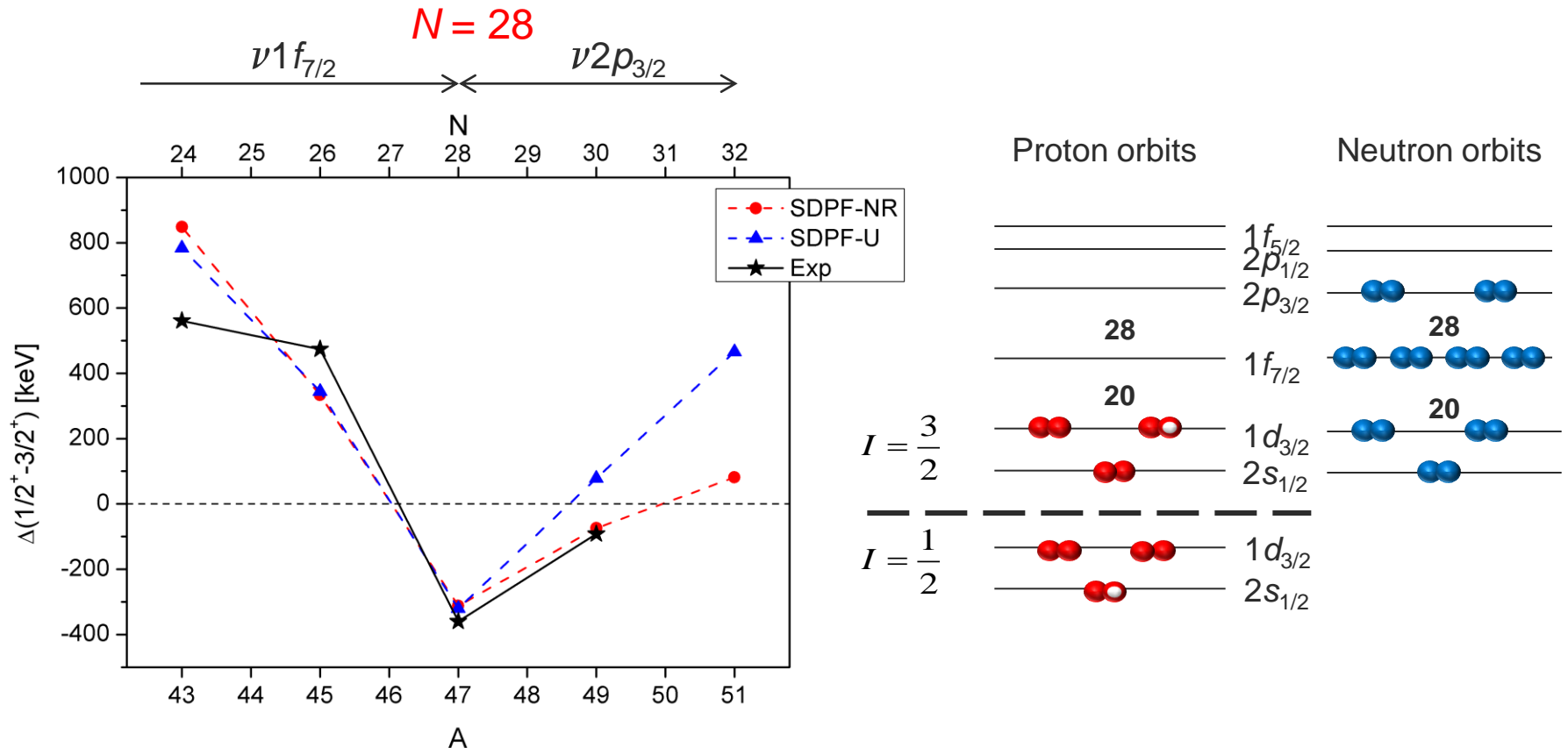


$^{48}\text{K}-^{51}\text{K}$

$^{40}\text{K}-^{47}\text{K}$

$^{36}\text{K}-^{39}\text{K}$

Motivation: Evolution of $3/2^+$ and $1/2^+$ states

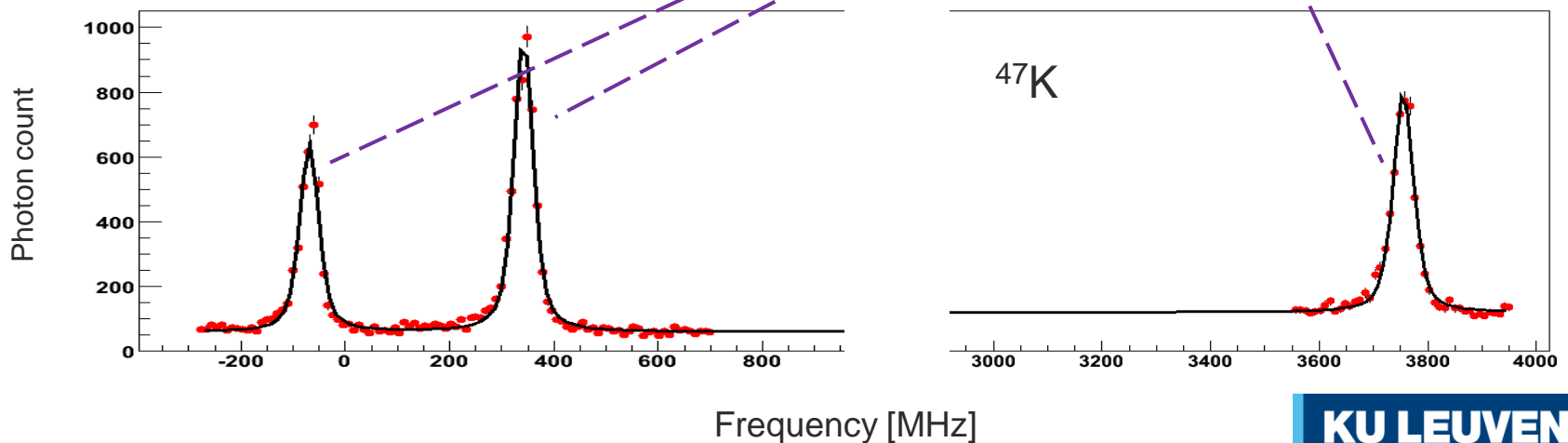
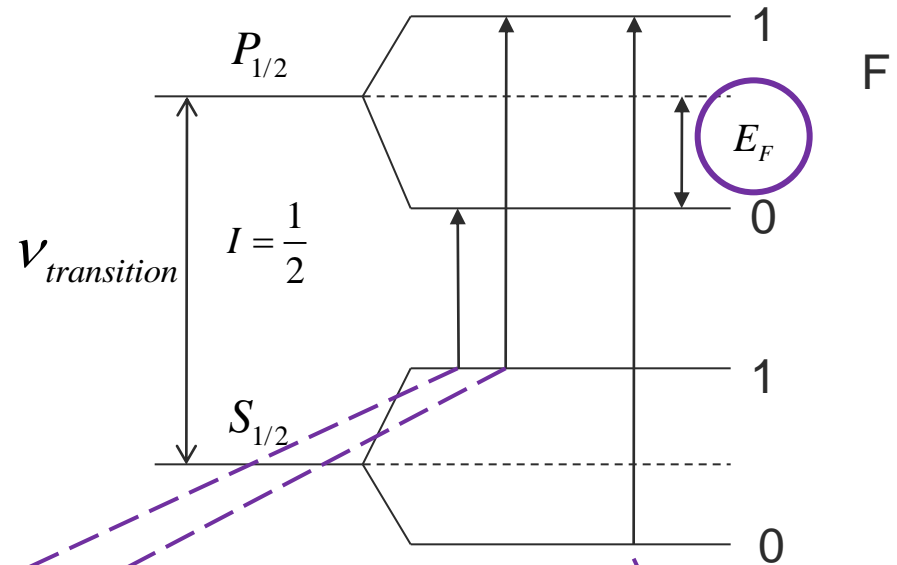


Collinear Laser Spectroscopy – measuring hyperfine splitting

- Hyperfine interaction couples the electron angular momentum (J) and nuclear spin (I)

- The total angular momentum:

$$\vec{F} = \vec{I} + \vec{J}$$



Collinear Laser Spectroscopy – measuring hyperfine splitting

- Energy difference: $E_F = \frac{1}{2}AC + B\frac{\frac{3}{4}C(C+1) - I(I+1)J(J+1)}{2I(I+1)J(J+1)}$ where $C = F(F+1) - I(I+1) - J(J+1)$

- Magnetic dipole HF parameter:

$$A = \frac{\mu_I B_J}{IJ}$$

- Electric quadrupole HF parameter:

$$B = eQV_{zz}$$

- Magnetic and quadrupole moment are deduced by relative measurement:

$$\mu = \frac{AI}{A_{ref}I_{ref}} \mu_{ref}$$

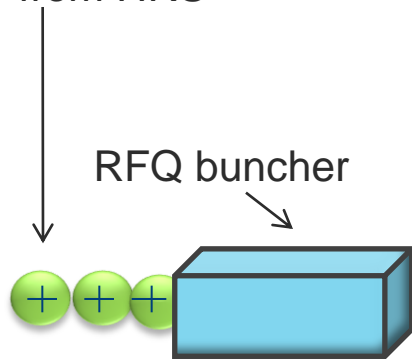
$$Q = \frac{B}{B_{ref}} Q_{ref}$$

- Mean square charge radii :

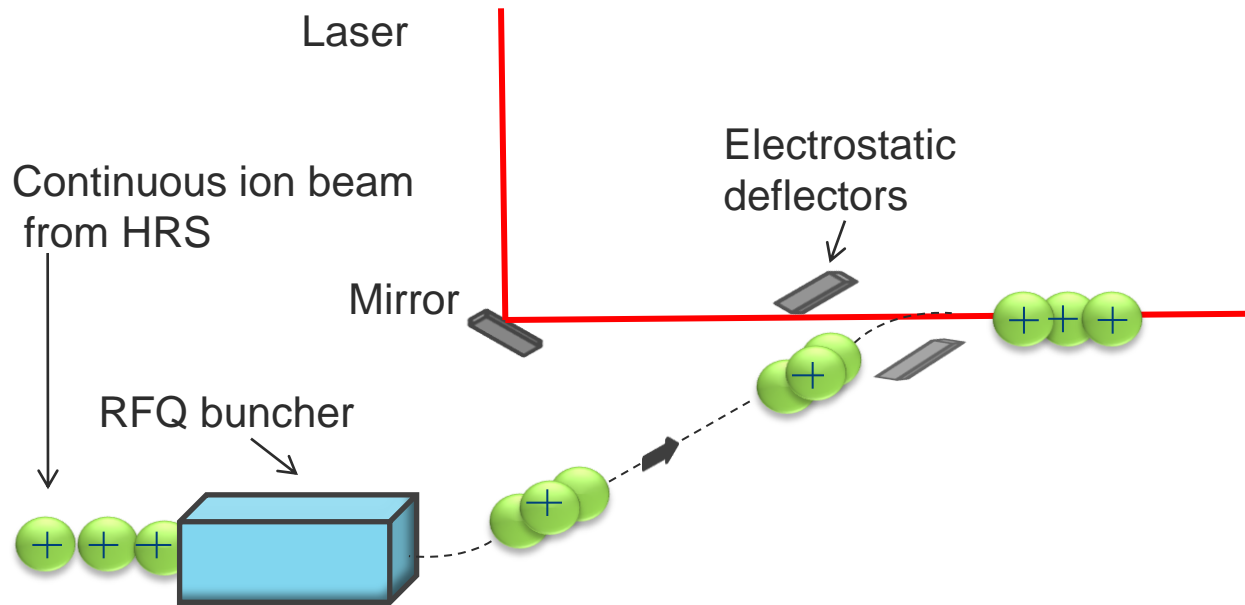
$$\delta\nu = \nu^A - \nu^{ref} = K \frac{m_A - m_{ref}}{m_A \cdot m_{ref}} + F \delta \langle r^2 \rangle$$

Setup – Collinear Laser Spectroscopy

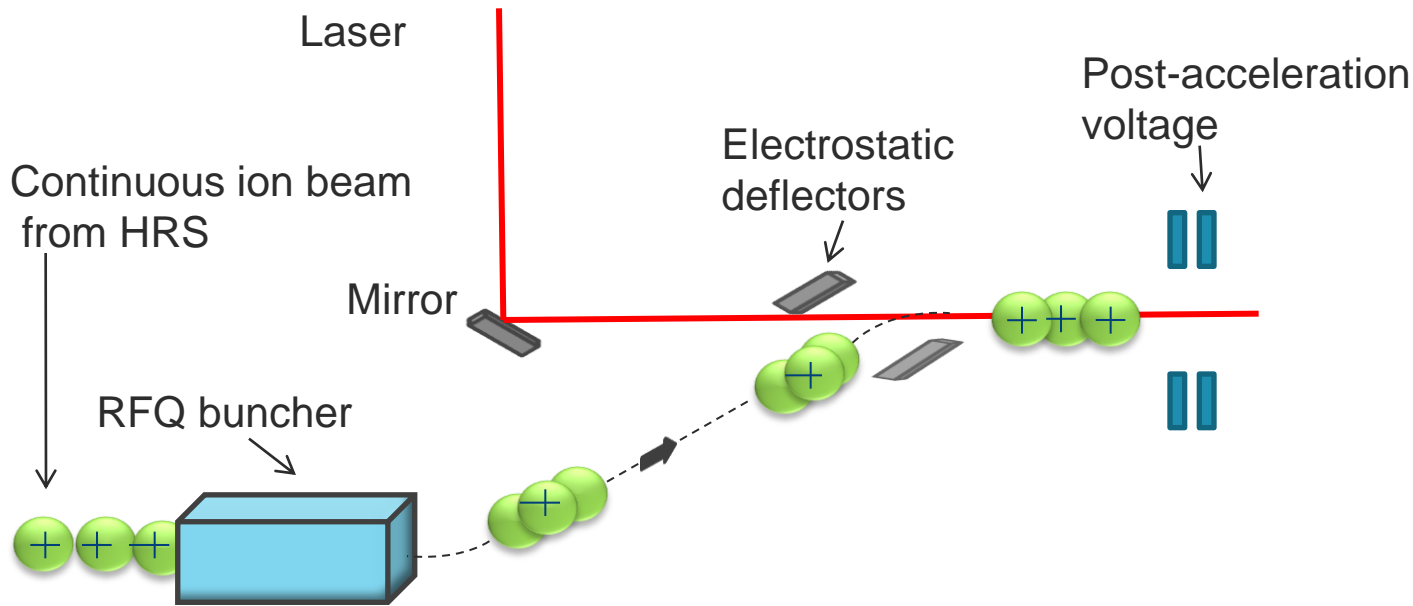
Continuous ion beam
from HRS



Setup – Collinear Laser Spectroscopy



Setup – Collinear Laser Spectroscopy

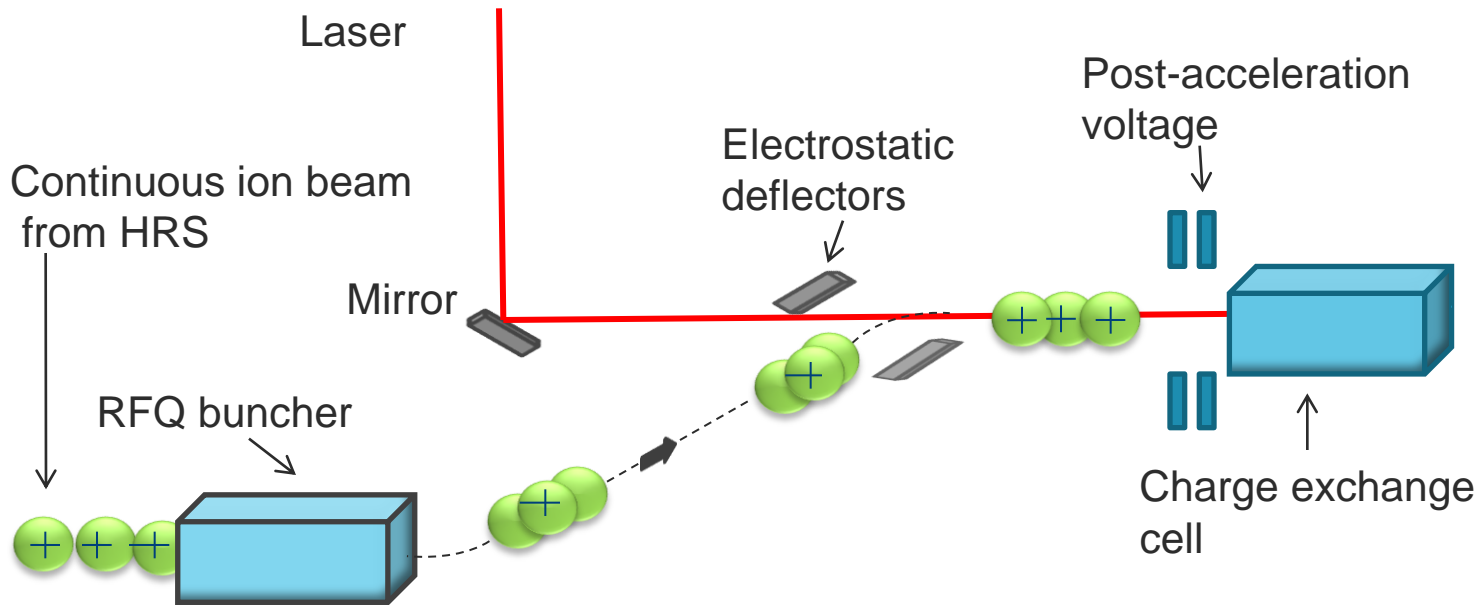


Doppler tuning:

$$v_{transition} = v_{laser} \frac{1 - \beta}{\sqrt{1 - \beta^2}}$$

$$\beta = \sqrt{1 - \frac{M_0^2 c^4}{(Uq + M_0 c^2)^2}}$$

Setup – Collinear Laser Spectroscopy

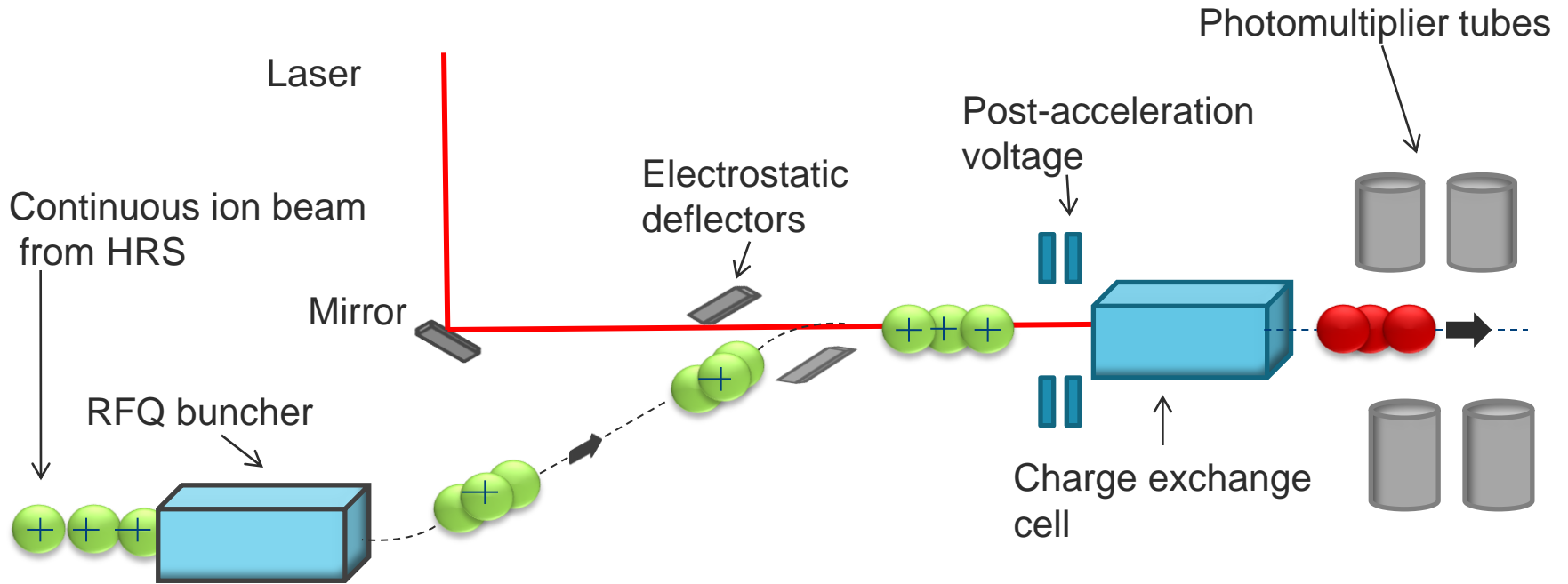


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Setup – Collinear Laser Spectroscopy

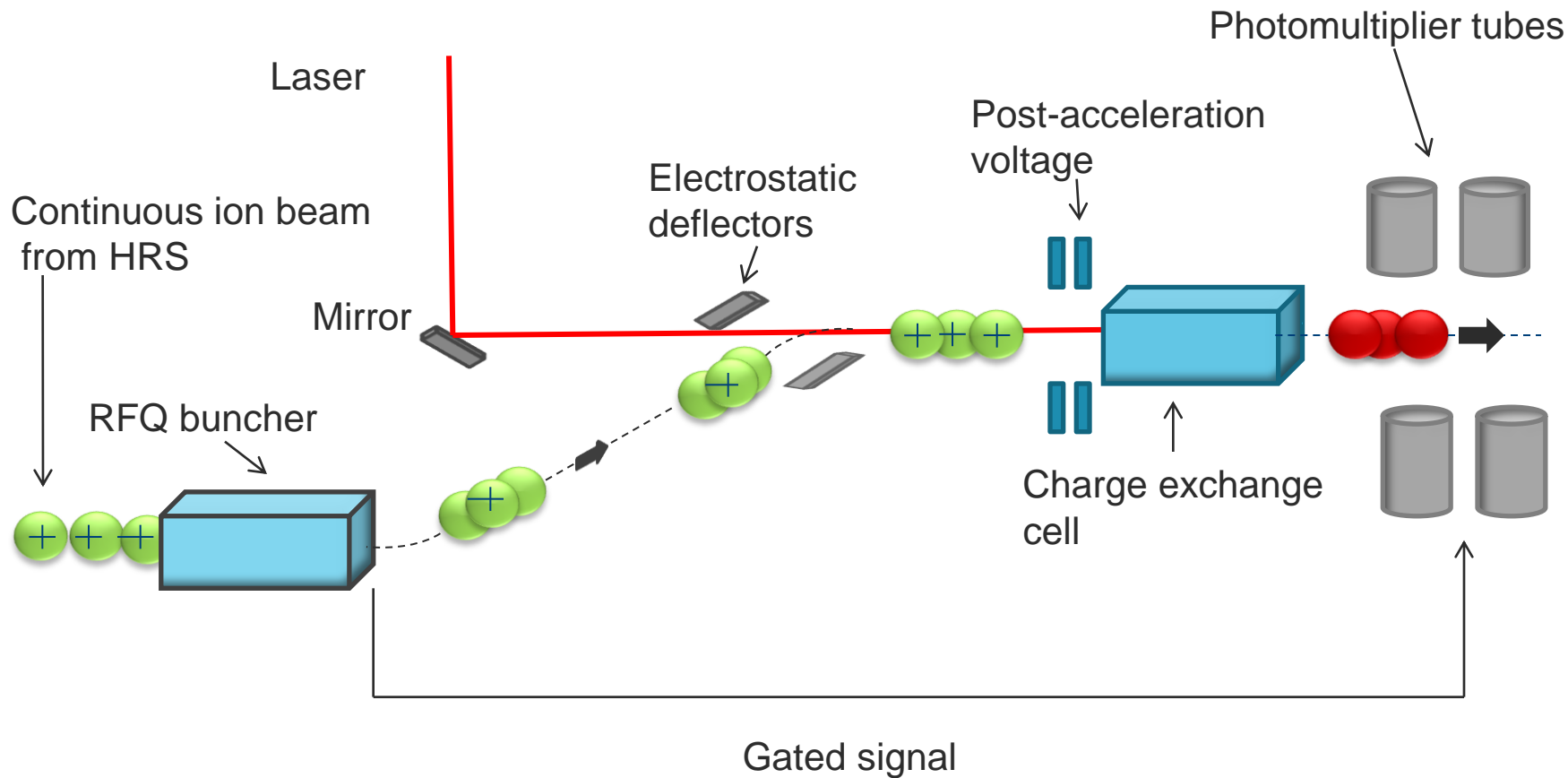


Doppler tuning:

$$v_{\text{transition}} = v_{\text{laser}} \frac{1 - \beta}{\sqrt{1 - \beta^2}}$$

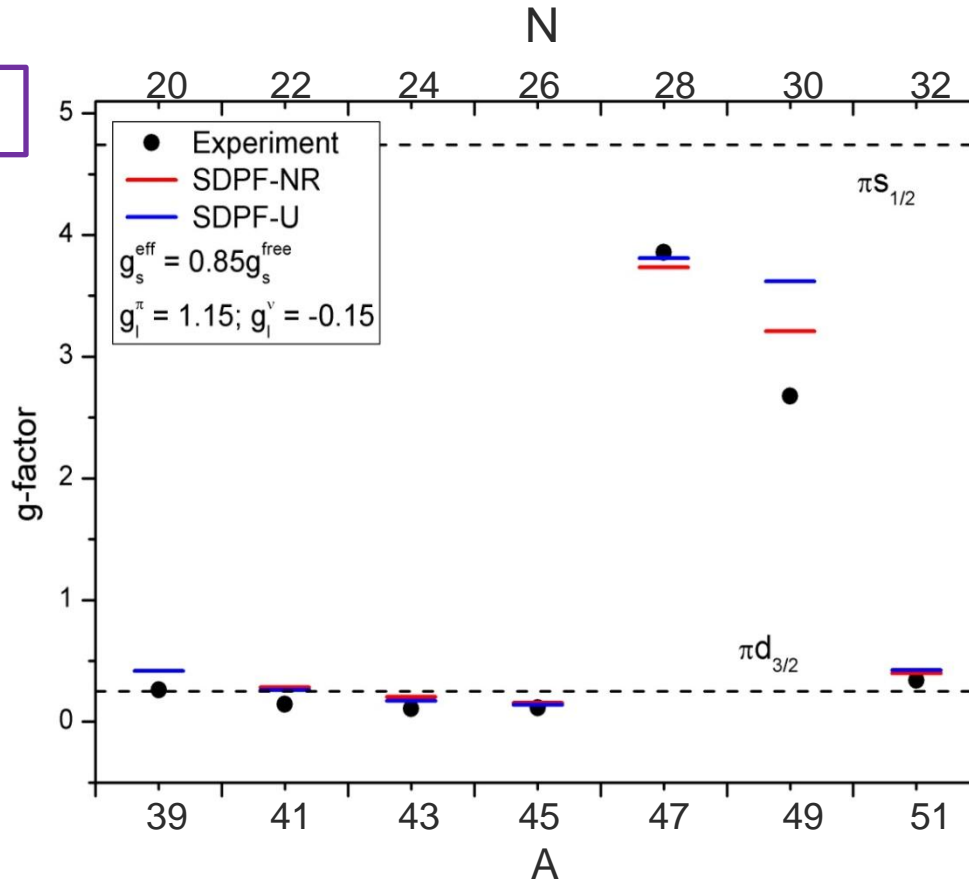
$$\beta = \sqrt{1 - \frac{M_0^2 c^4}{(Uq + M_0 c^2)^2}}$$

Setup – Collinear Laser Spectroscopy



Magnetic moment of odd-K (odd-even) isotopes

$$g = \frac{\mu}{I}$$



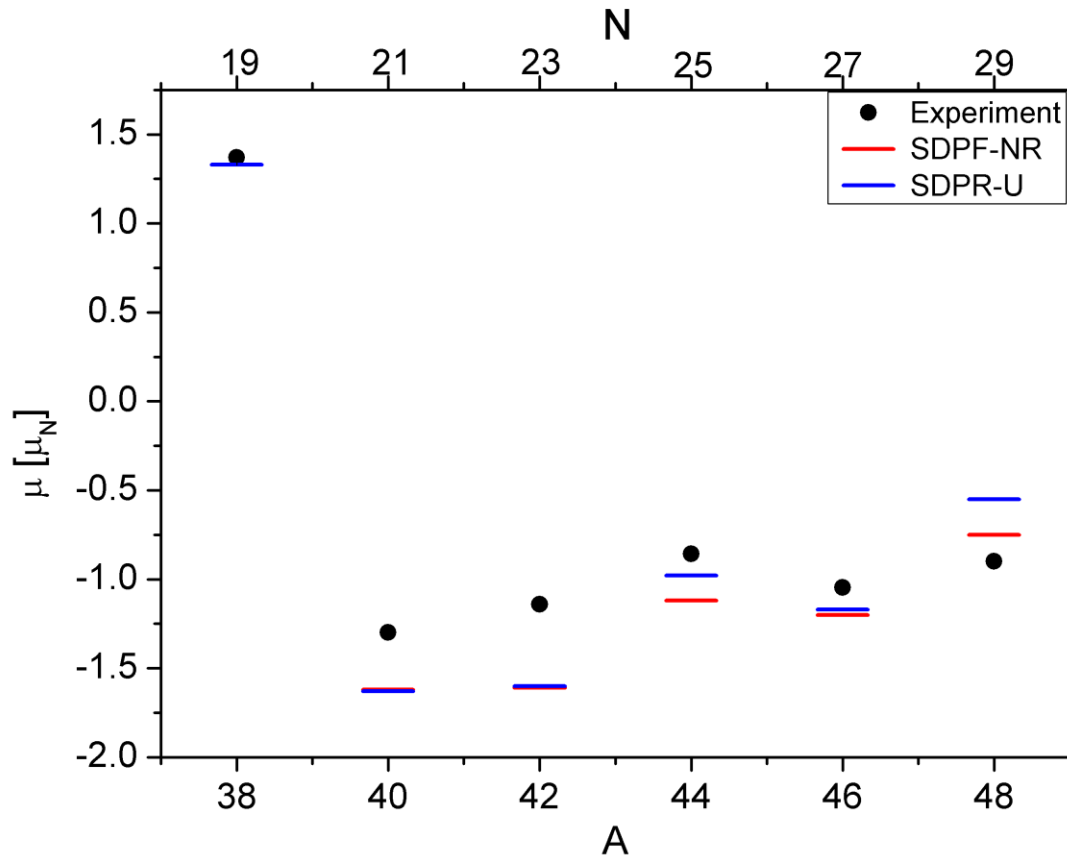
Spin determination

- ^{49}K :
3 peaks $\Rightarrow I = 1/2$
- ^{51}K :
4 peaks $\Rightarrow I > 1/2$
 $I = 3/2$ from intensities ratio

----- Effective single-particle g factor

- ^{47}K : $\sim 13\%$ mixing with $\pi d_{3/2}^{-1} - \nu(pf)$
- ^{49}K : $\sim 20\%$ from SDPF-NR and $\sim 15\%$ from SDPF-U
more mixing is needed

Magnetic moment for even-K (odd-odd) isotopes



Spin determination

- ^{48}K :
 $I = 1$ from intensities ratio
- ^{50}K :
 $I = 0 \Rightarrow$ single peak

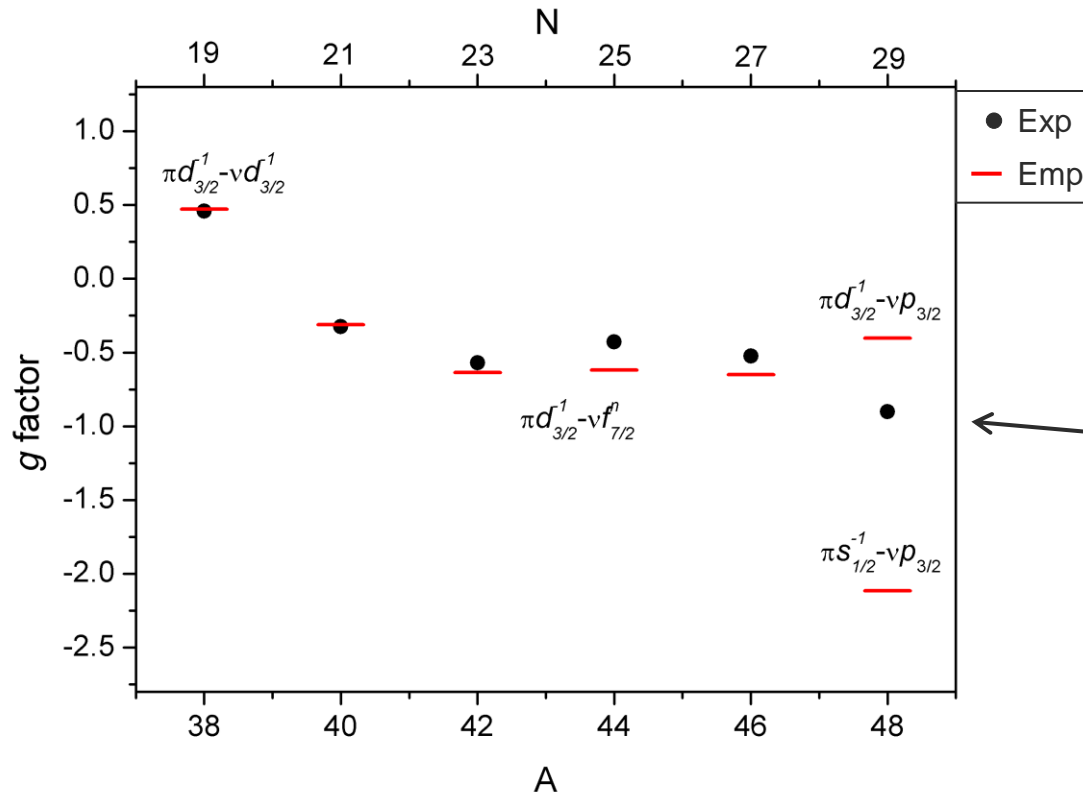
Empirical magnetic moments

- Additivity rule for odd-odd isotopes:

$$g(I) = \frac{g(j_\pi) + g(j_\nu)}{2} + \frac{g(j_\pi) - g(j_\nu)}{2} \frac{j_\pi(j_\pi + 1) - j_\nu(j_\nu + 1)}{I(I + 1)}$$

$g(j_\pi)$: odd-even K isotopes

$g(j_\nu)$: even-odd Ca isotopes ($Z = 20$)



^{48}K : mixed configuration

Conclusions

- For the first time, the hyperfine spectra for $^{48-51}\text{K}$ were obtained
- The ground state spins were deduced for $^{48-51}\text{K}$
- From the magnetic moments (g factors) \Rightarrow the composition of the wave function
- The gap between proton $1d_{3/2}$ and $2s_{1/2}$ orbits reaches a minimum around $N = 29$ and again increases towards the more neutron-rich K isotopes

COLLAPS collaboration



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²*Max-Planck-Institut für Kernphysik, D-69117 Heidelberg, Germany*

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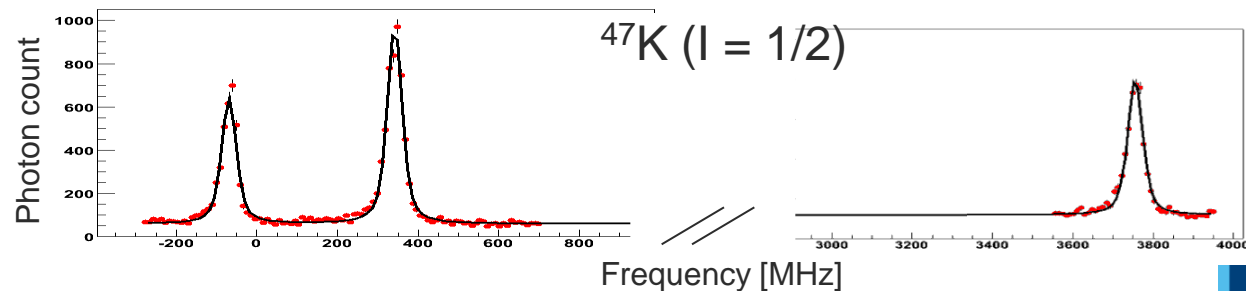
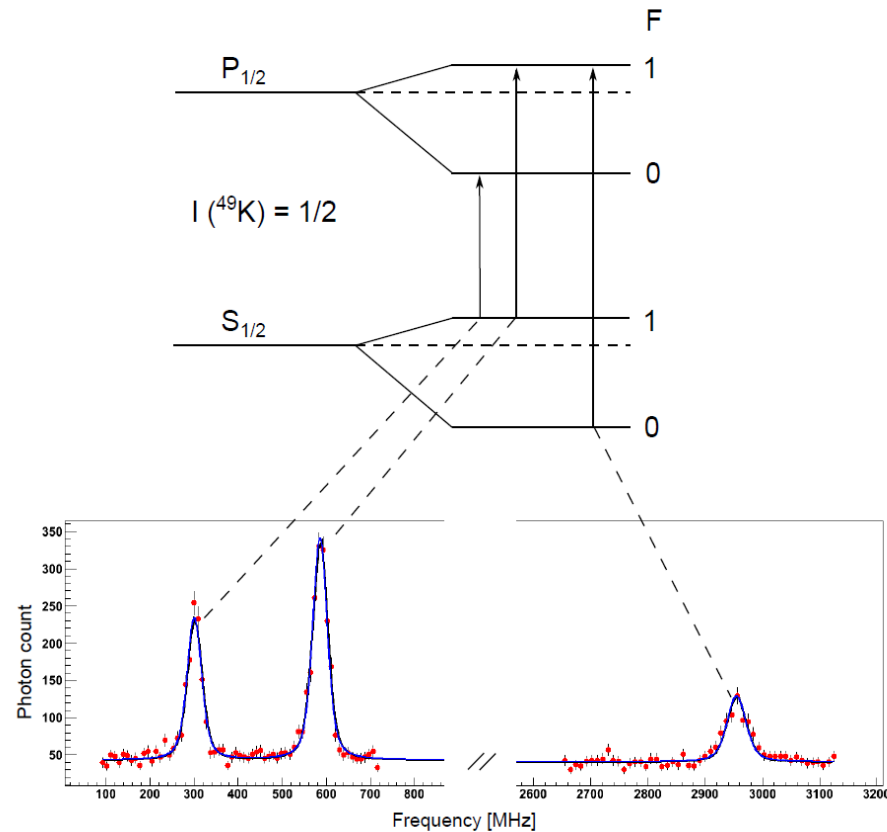
⁵*Institut für Kernphysik, TU Darmstadt, D-64289 Darmstadt, Germany*

⁶*GSI Helmholtzzentrum für Schwerionenforschung, D-64291 Darmstadt, Germany*

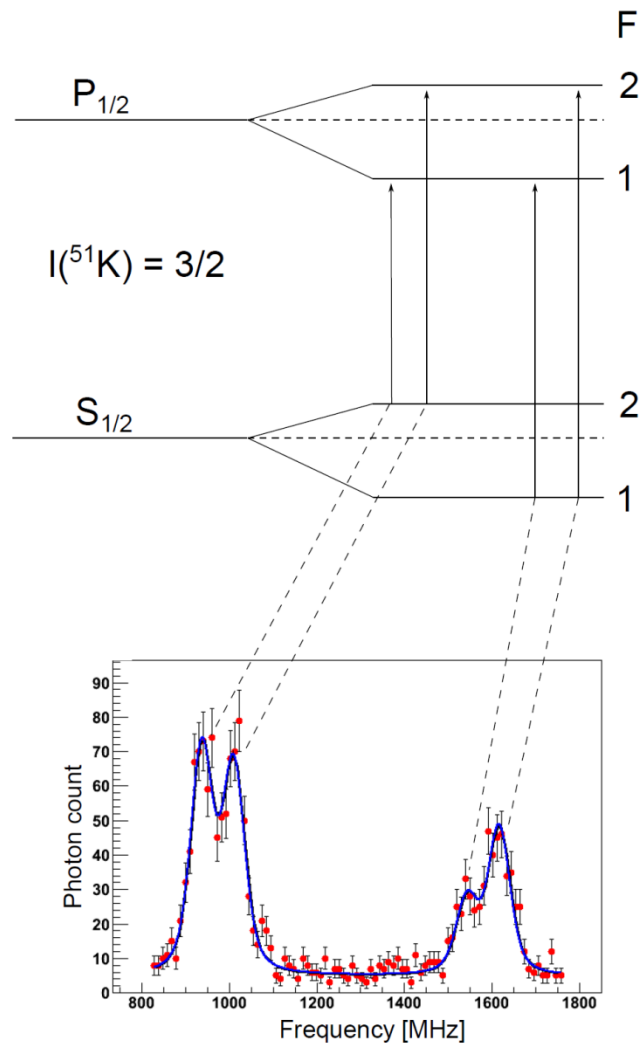
Thank you for your attention!

Spin determination of ^{49}K

3 peaks $\Rightarrow I = 1/2$

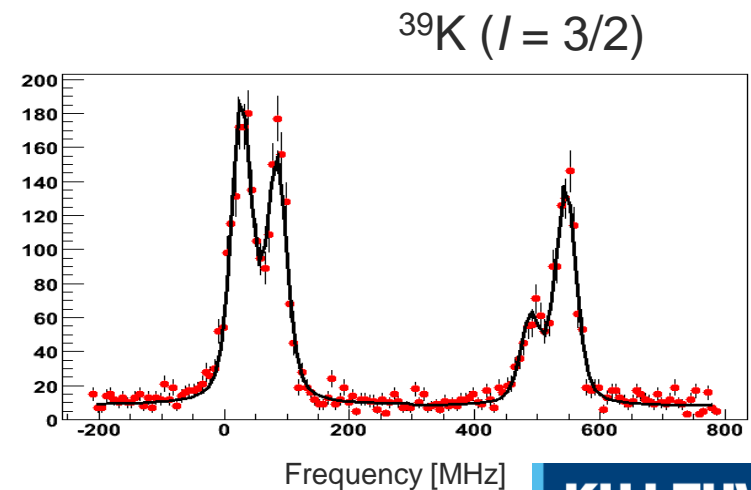


Spin determination of ^{51}K

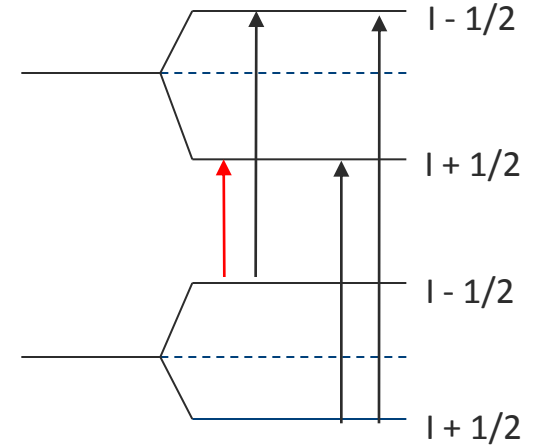
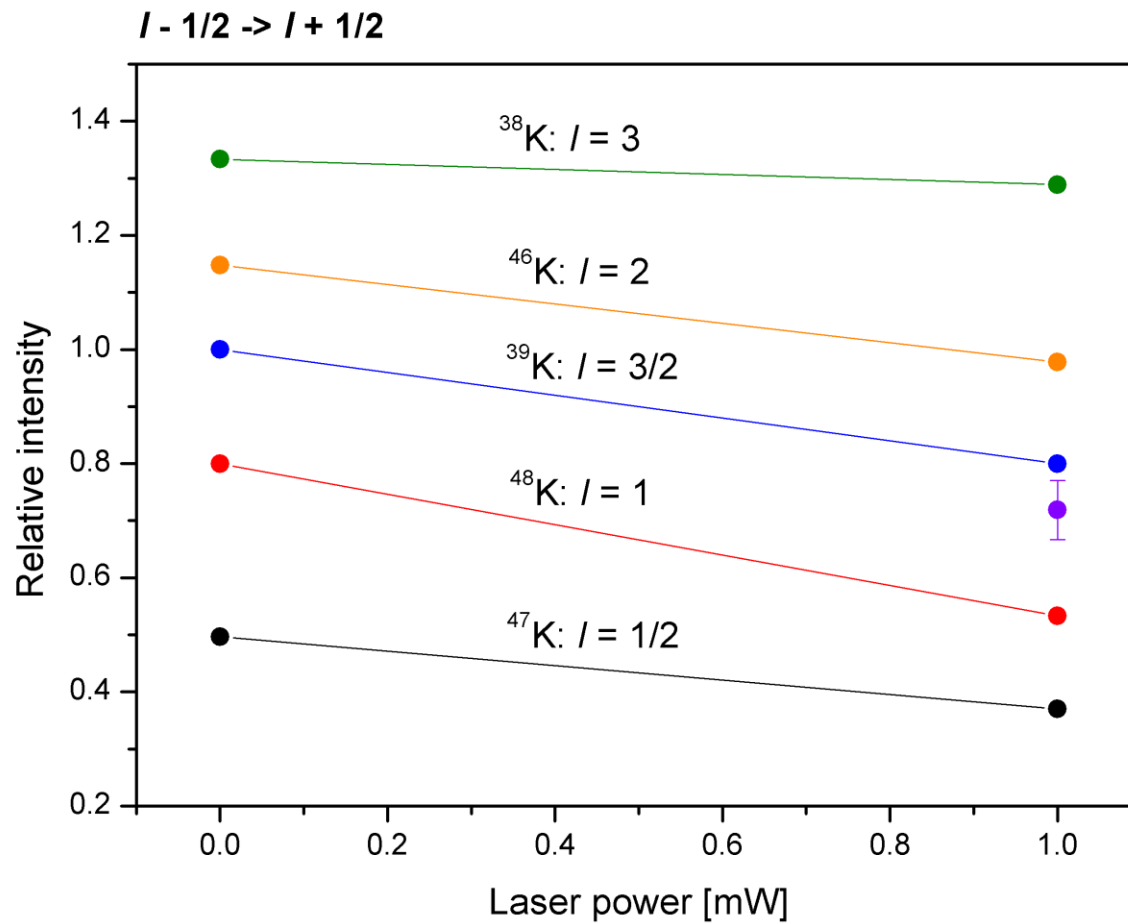


4 peaks $\Rightarrow I > 1/2$

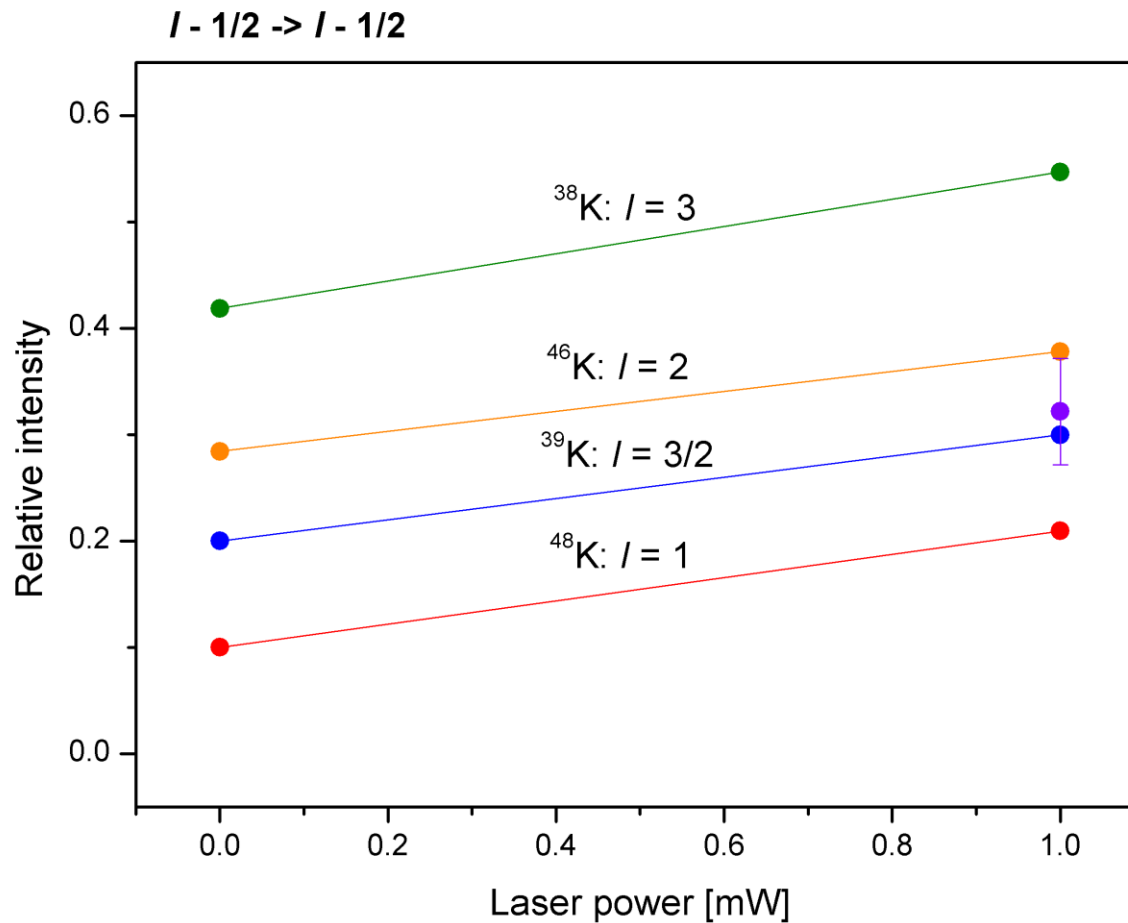
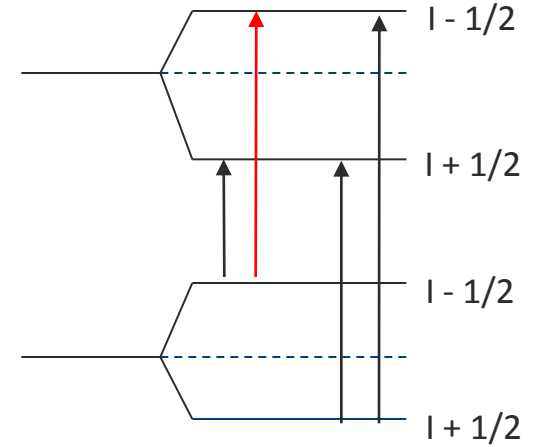
$I = 3/2$ from intensities ratio



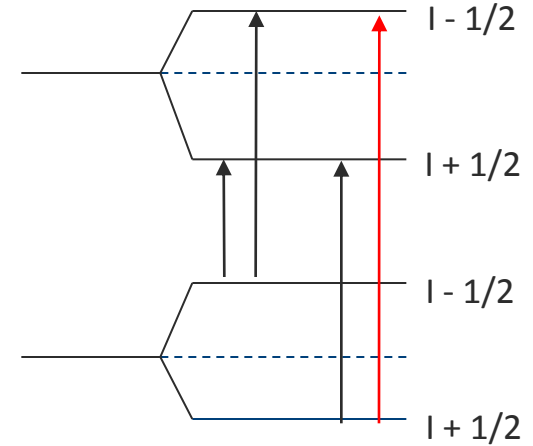
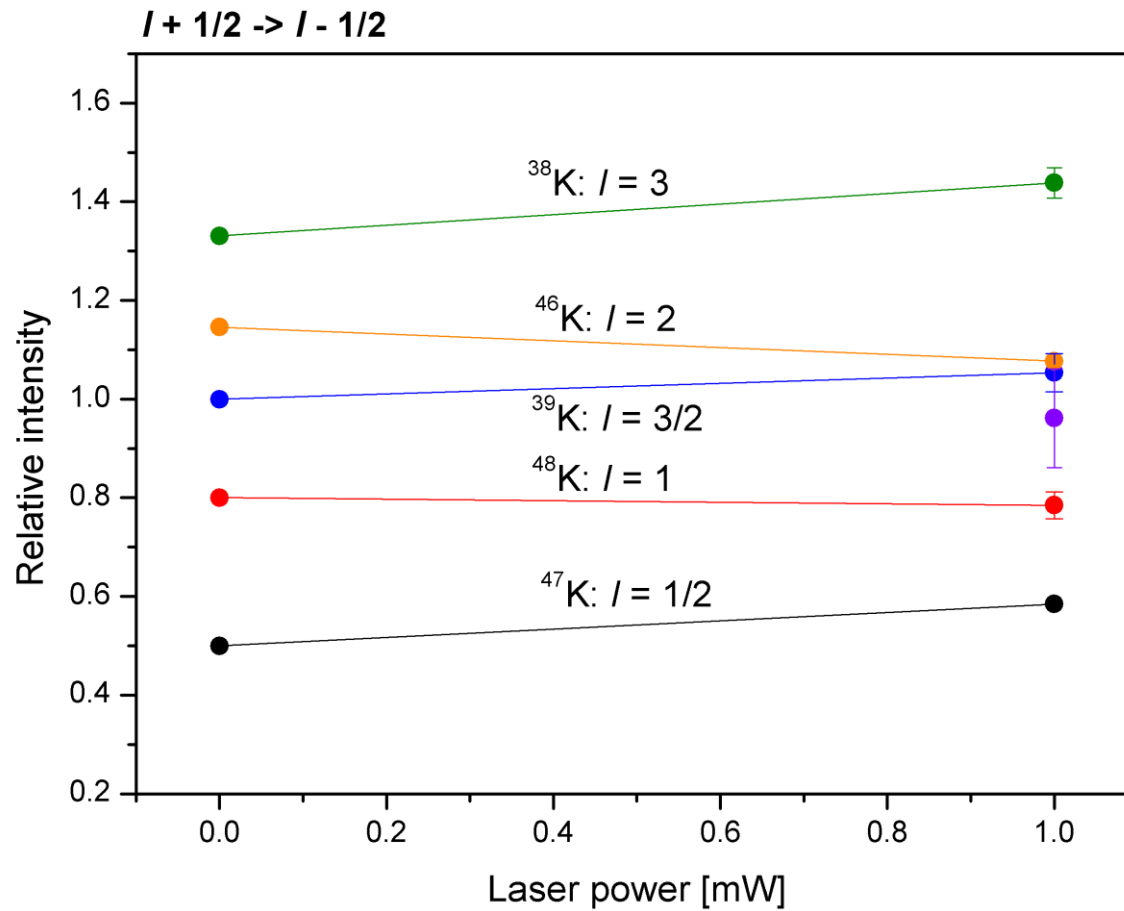
Spin determination of ^{51}K



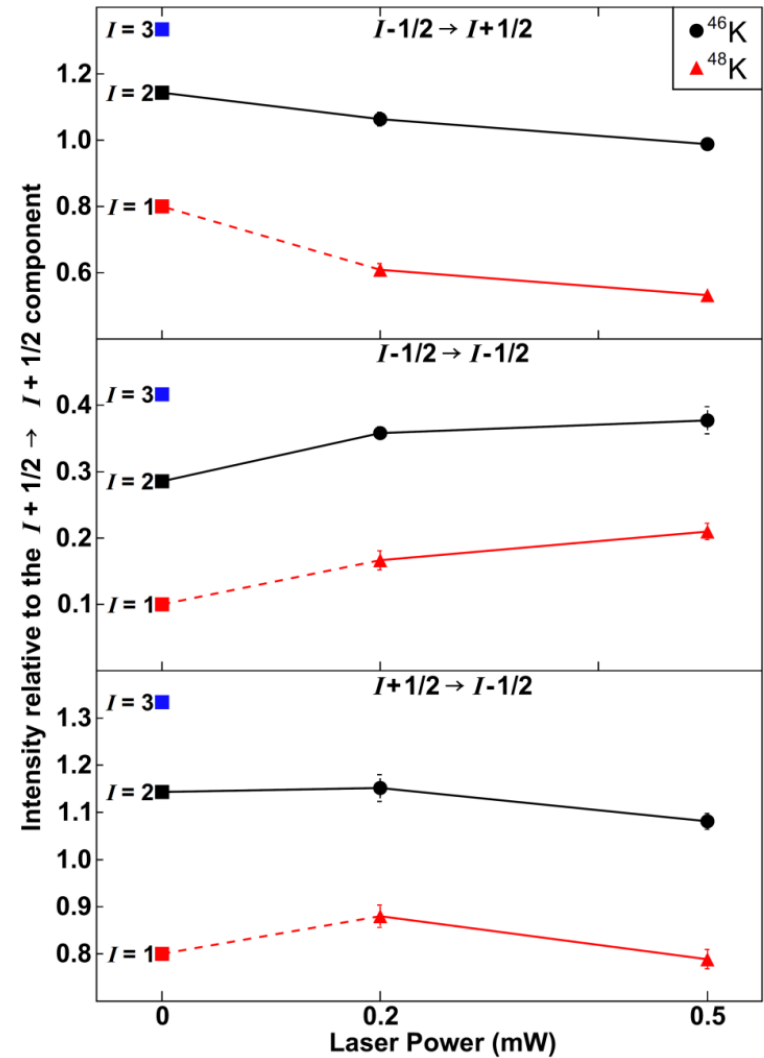
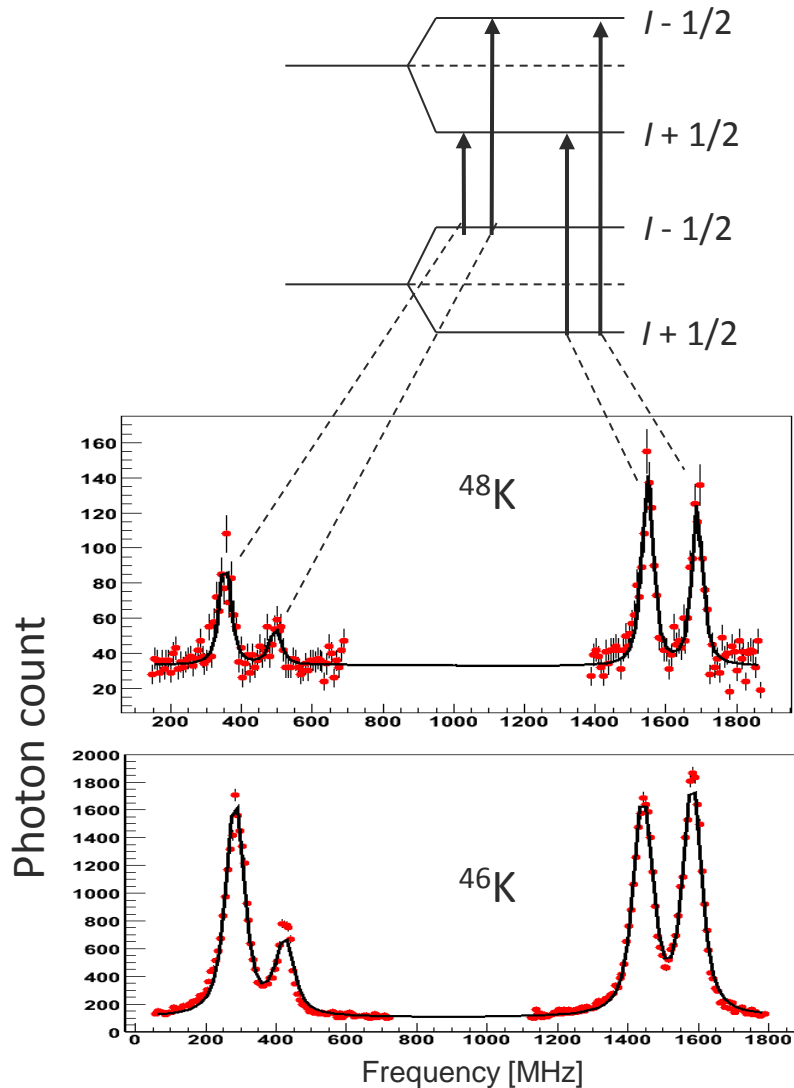
Spin determination of ^{51}K



Spin determination of ^{51}K

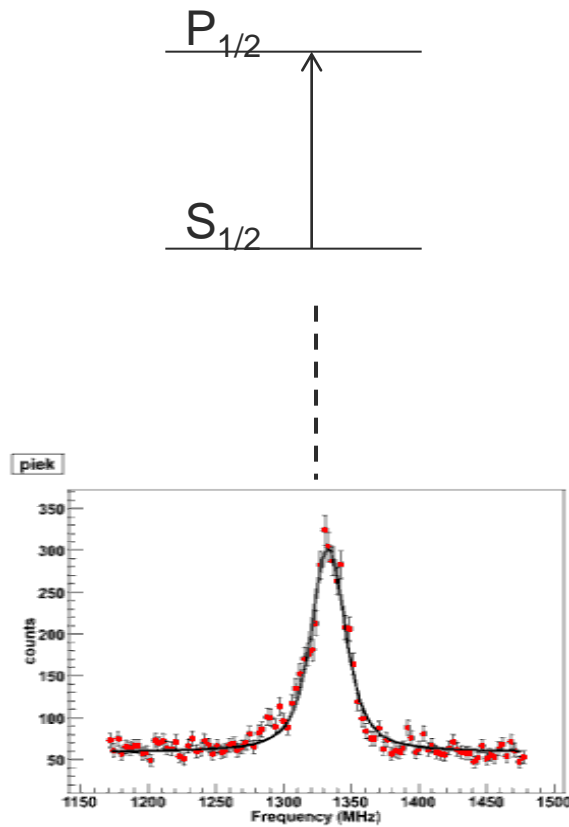


Spin determination of ^{48}K

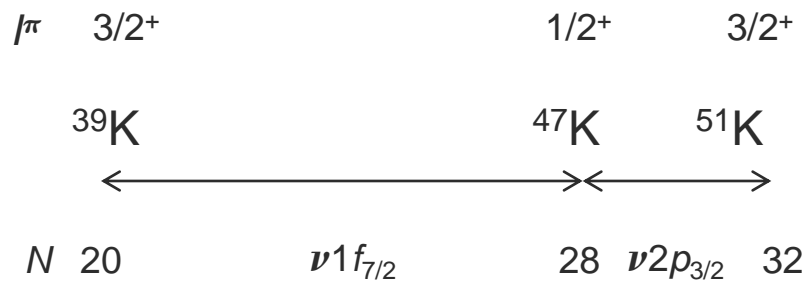
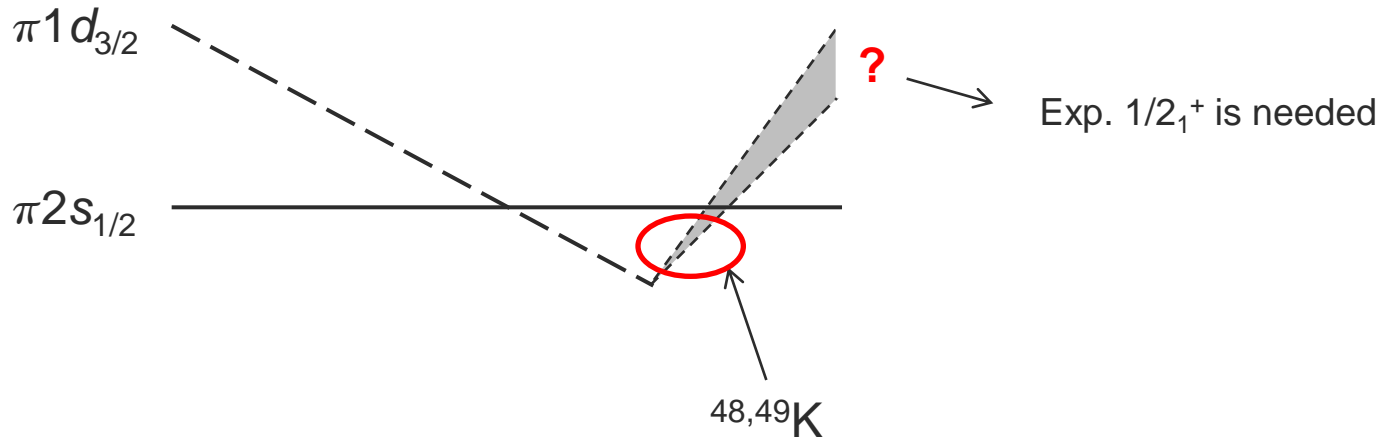


Spin determination of ^{50}K

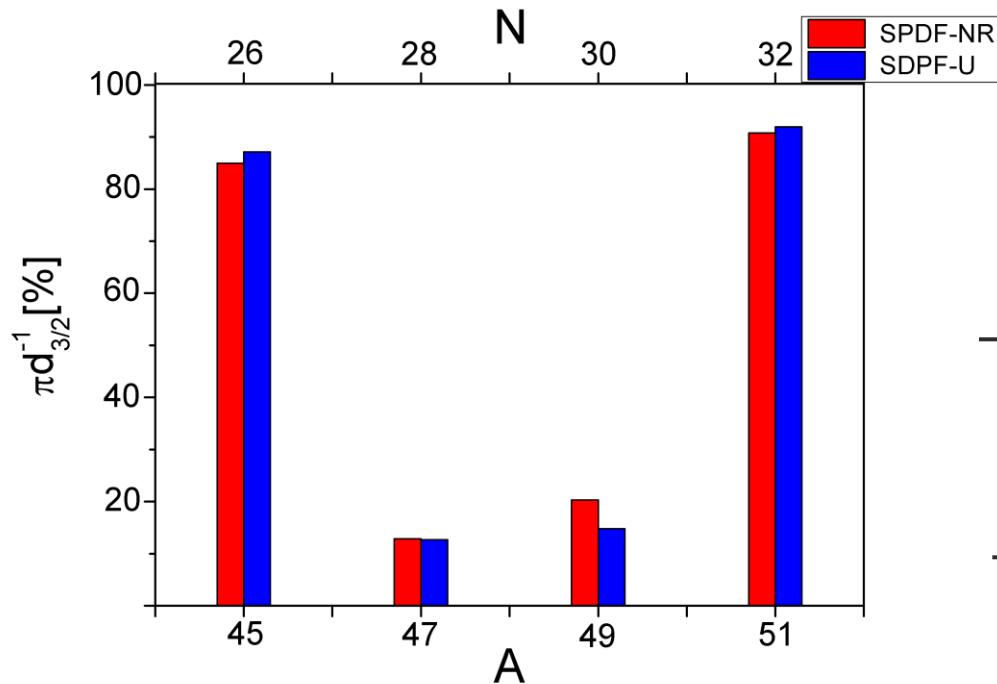
$I = 0 \Rightarrow$ single peak



Monopole interaction



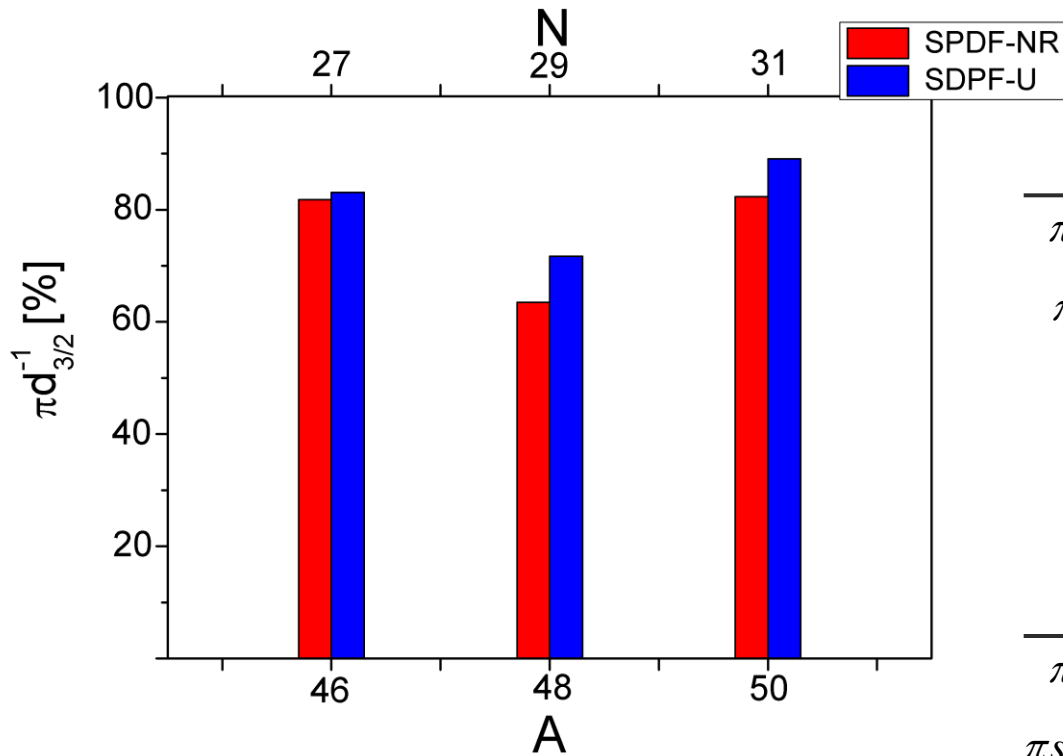
Composition of the wave function of odd-K



⁴⁷ K	SDPF-NR	SDPF-U
$\pi d_{3/2}^{-1} \otimes \nu(fp)$	13%	13%
⁴⁹ K	SDPF-NR	SDPF-U
$\pi d_{3/2}^{-1} \otimes \nu(fp)$	20%	15%

- ⁴⁹K: more mixing is needed (~25%)

Composition of the wave function of even-K



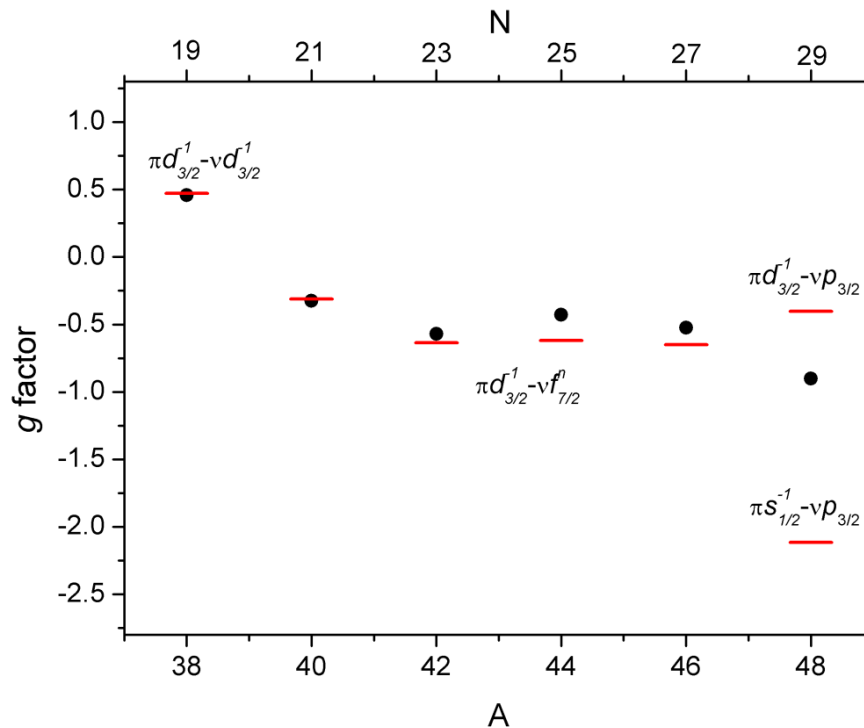
^{48}K	SDPF-NR	SDPF-U
$\pi d_{3/2}^{-1} \otimes \nu p_{3/2}$	38%	51%
$\pi s_{1/2}^{-1} \otimes \nu p_{3/2}$	16%	14%

^{50}K	SDPF-NR	SDPF-U
$\pi d_{3/2}^{-1} \otimes \nu p_{3/2}^{-1}$	63%	75%
$\pi s_{1/2}^{-1} \otimes \nu p_{3/2}^2 p_{1/2}$	7%	> 5%

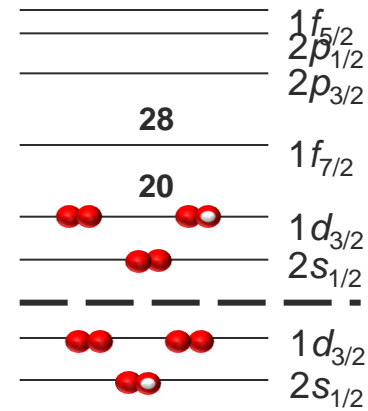
Empirical magnetic moments

- Additivity rule for odd-odd isotopes:

$$g(I) = \frac{g(j_\pi) + g(j_\nu)}{2} + \frac{g(j_\pi) - g(j_\nu)}{2} \frac{j_\pi(j_\pi + 1) - j_\nu(j_\nu + 1)}{I(I + 1)}$$

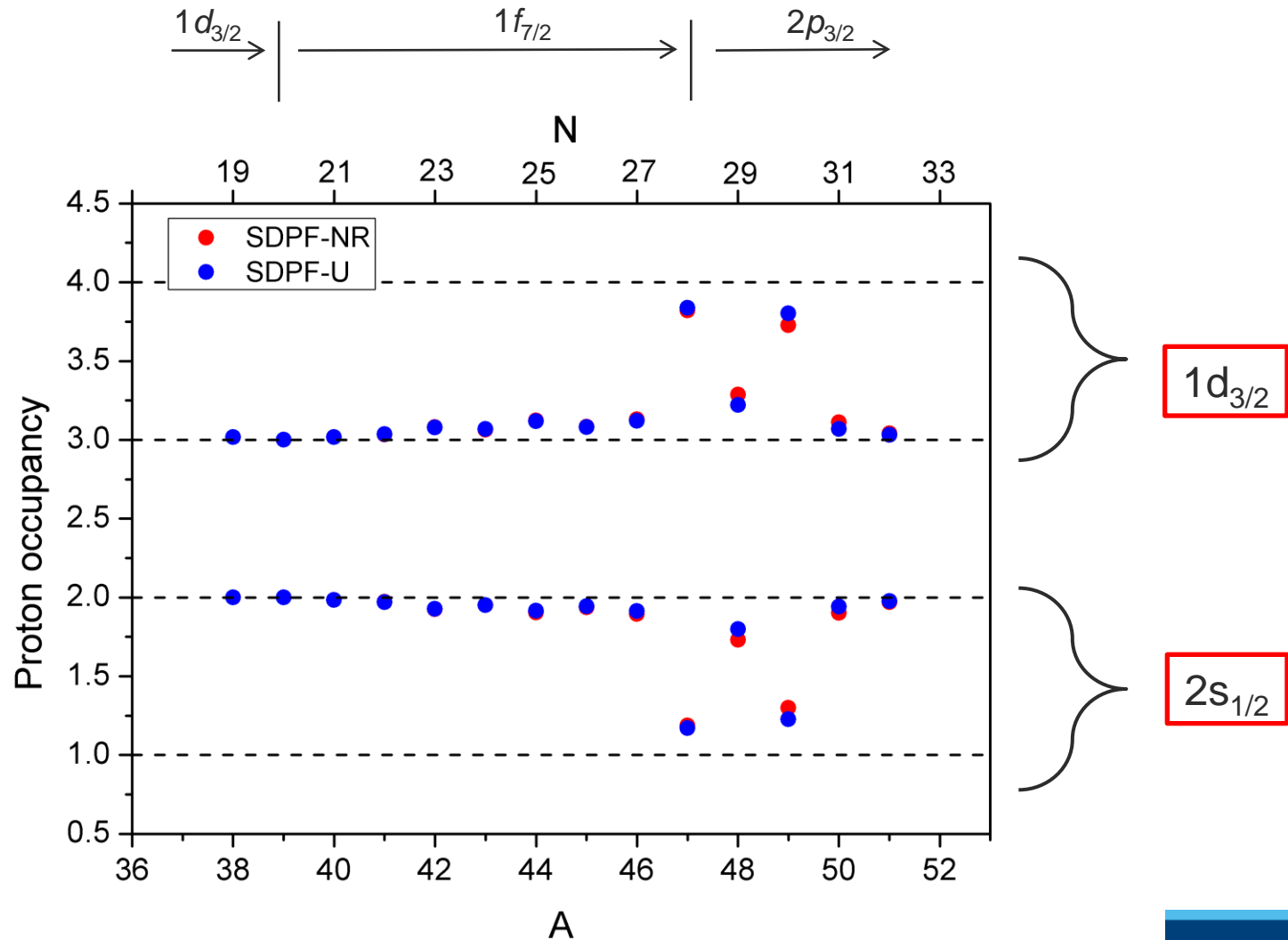


Proton orbits



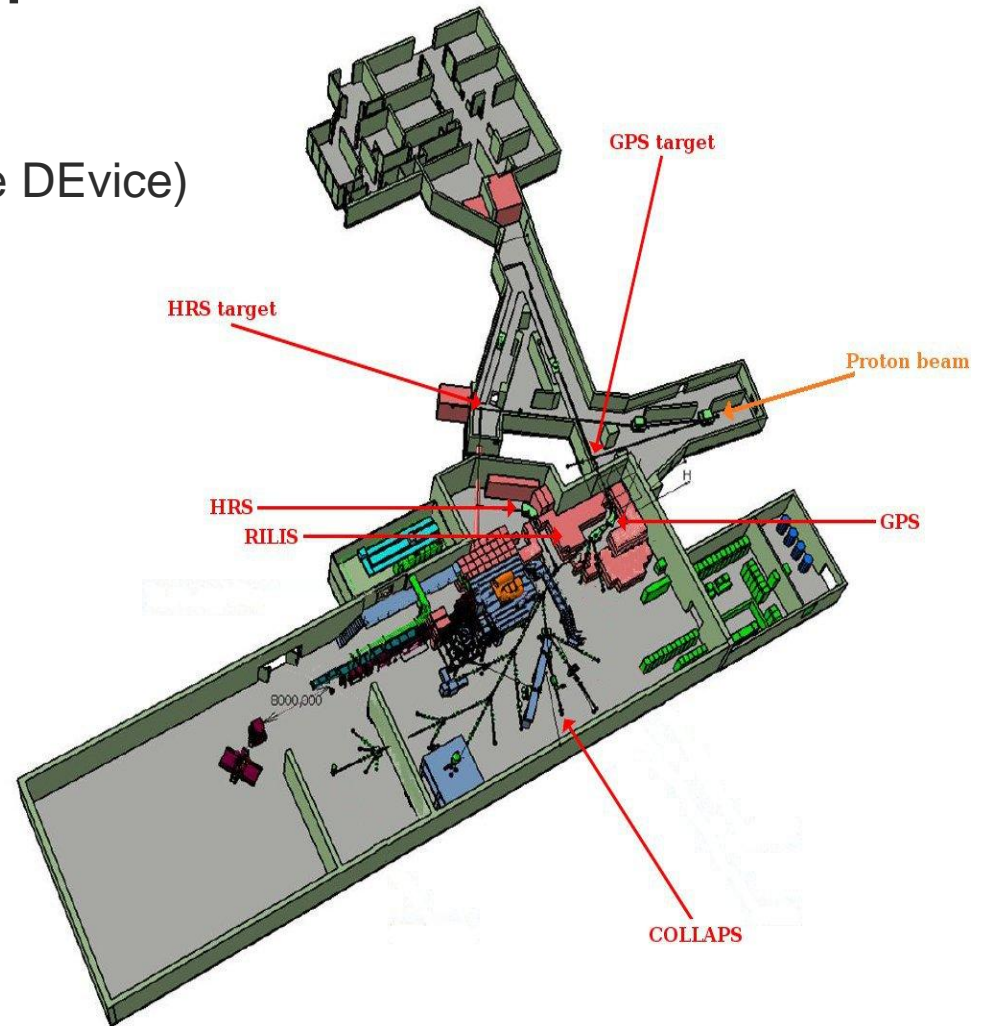
Isotope	I^π	configuration	g_{emp}	used isotopes
^{38}K	3^+	$\pi 1d_{3/2}^{-1} \otimes \nu 1d_{3/2}^{-1}$	+0.47	(^{39}K ; ^{39}Ca)
^{40}K	4^-	$\pi 1d_{3/2}^{-1} \otimes \nu 1f_{7/2}$	-0.31	(^{39}K ; ^{41}Ca)
^{42}K	2^-	$\pi 1d_{3/2}^{-1} \otimes \nu 1f_{7/2}^3$	-0.64	(^{41}K ; ^{43}Ca)
^{44}K	2^-	$\pi 1d_{3/2}^{-1} \otimes \nu 1f_{7/2}^5$	-0.62	(^{43}K ; ^{45}Ca)
^{46}K	2^-	$\pi 1d_{3/2}^{-1} \otimes \nu 1f_{7/2}^{-1}$	-0.65	(^{45}K ; ^{47}Ca)
^{48}K	1^-	$\pi 1d_{3/2}^{-1} \otimes \nu 2p_{3/2}$	-0.40	(^{45}K ; ^{49}Ca)
^{48}K	1^-	$\pi 2s_{1/2}^{-1} \otimes \nu 2p_{3/2}$	-2.11	(^{47}K ; ^{49}Ca)

Occupation

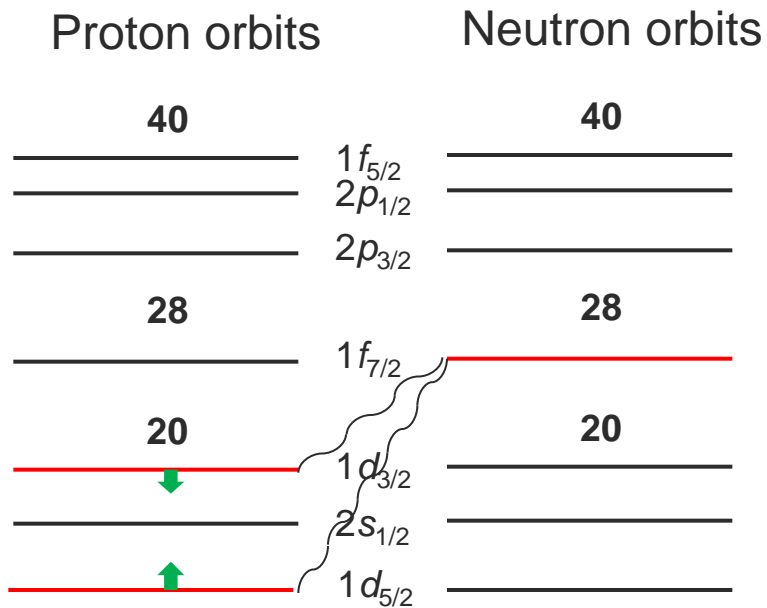


Setup – Ion beam

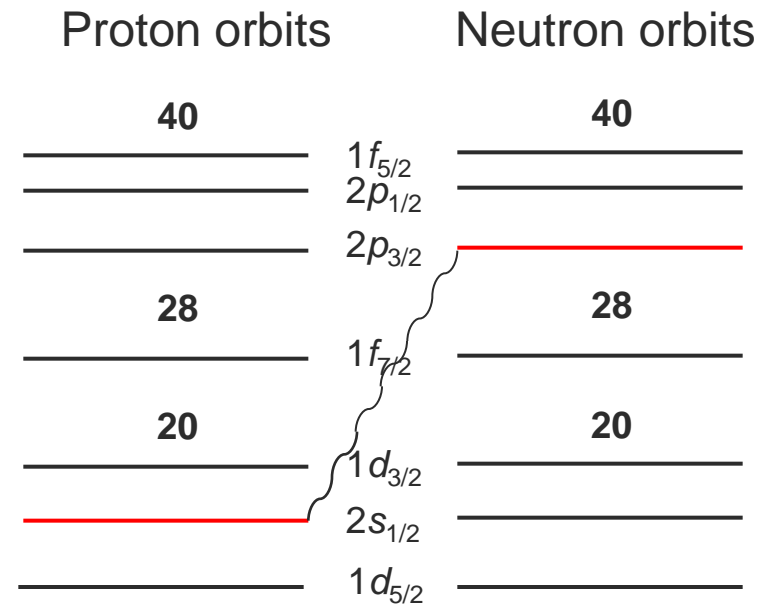
- ISOLDE (Isotope Separator On-Line DEvice)
- Protons (1.4GeV) on UC_x target
- Ionization by Surface Ion Source
- Ions accelerated up to 60 keV
- HRS (High Resolution Separation)



Tensor part



Central part



- $n = n'$ and $l = l' \Rightarrow$ maximal overlap of the WF
- Spin-dependent: $j_> = l + 1/2$ and $j_< = l - 1/2$
 $(j_> \text{ and } j_<) \text{ is stronger than } (j_> \text{ and } j_>) \text{ or } (j_< \text{ and } j_<)$

Magnetic moments - results

Isotope	I^π	μ_{exp}	$\mu_{\text{SDPF-NR}}$	$\pi 1d_{3/2}^{-1}$ [%]	$\mu_{\text{SDPF-U}}$	$\pi 1d_{3/2}^{-1}$ [%]	μ_{lit}	Reference
^{39}K	$3/2^+$	+0.3917 (5) [12]	+0.65	95%	+0.65	95%	+0.3914662 (3)	[29]
^{41}K	$3/2^+$	-	+0.42	92%	+0.38	92%	+0.2148701 (2)	[29]
^{43}K	$3/2^+$	-	+0.27	88%	+0.22	88%	+0.1633 (8) ^a	[27]
^{45}K	$3/2^+$	-	+0.26	85%	+0.24	87%	+0.1734 (8) ^a	[27]
^{47}K	$1/2^+$	+1.92924 (11) [58]	+1.86	13%	+1.91	13%	+1.933(9) ^a	[27]
^{49}K	$1/2^+$	+1.3386 (8) [40]	+1.63	20%	+1.82	15%	-	-
^{51}K	$3/2^+$	+0.5129 (22) [15]	+0.59	91%	+0.63	92%	-	-

Isotope	I^π	μ_{exp}	$\mu_{\text{SDPF-NR}}$	$\mu_{\text{SDPF-U}}$	μ_{lit}	Reference
^{38}K	3^+	+1.3703 (6) [41]	+1.33	+1.33	+1.371 (6) ^a	[27]
^{40}K	4^-	-	-1.62	-1.63	-1.2964 (4) ^b	[31]
^{42}K	2^-	-1.1393 (3) [34]	-1.61	-1.60	-1.14087 (20) ^b	[28]
^{44}K	2^-	-0.8569 (5) [26]	-1.12	-0.98	-0.856 (4) ^a	[27]
^{46}K	2^-	-1.0464 (5) [31]	-1.20	-1.17	-1.051 (6) ^a	[27]
^{48}K	1^-	-0.8997 (3) [27]	-0.75	-0.55	-	-

[27] F. Touchard *et al.*, Phys. Lett. B **108**, 169 (1982).

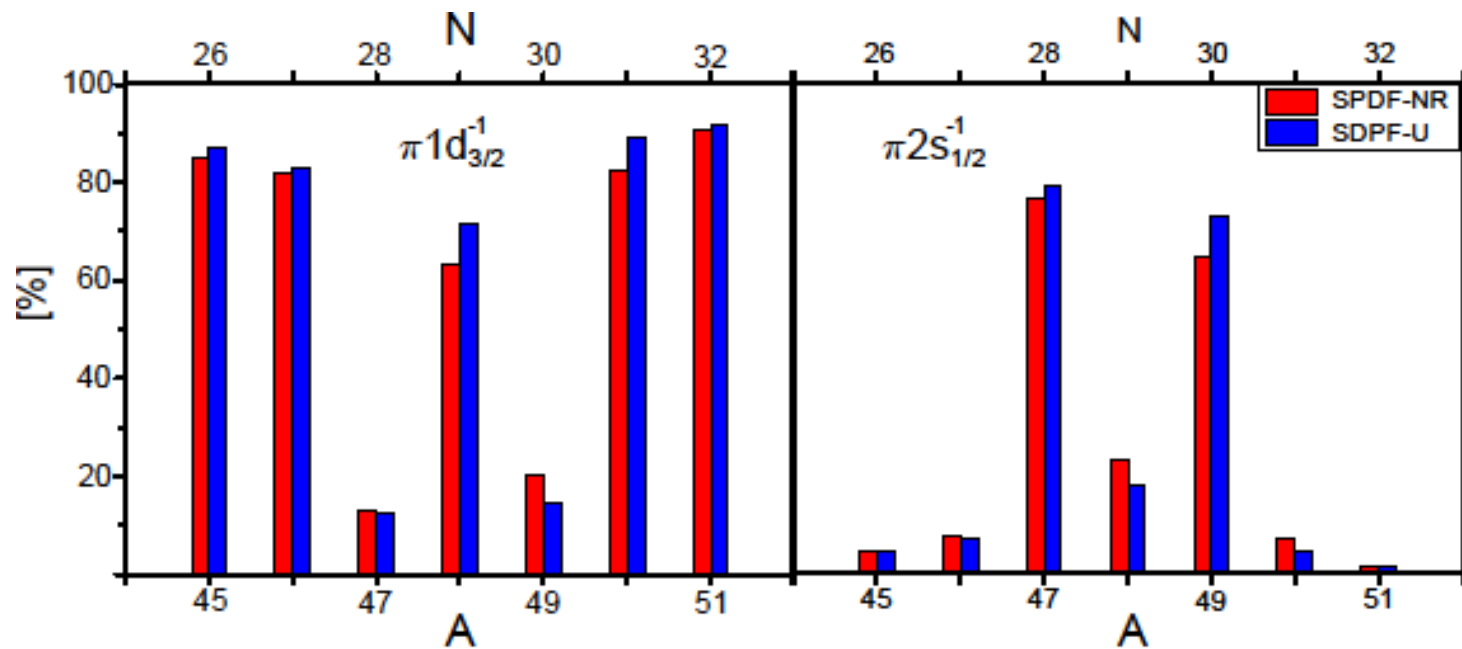
[28] Y. W. Chan, V. W. Cohen, and H. B. Silsbee, Phys. Rev. **184**, 1102 (1969).

[29] A. Beckmann, K. D. Böklen, and D. Elke, Zeitschrift für Physik A Hadrons and Nuclei **270**, 173 (1974).

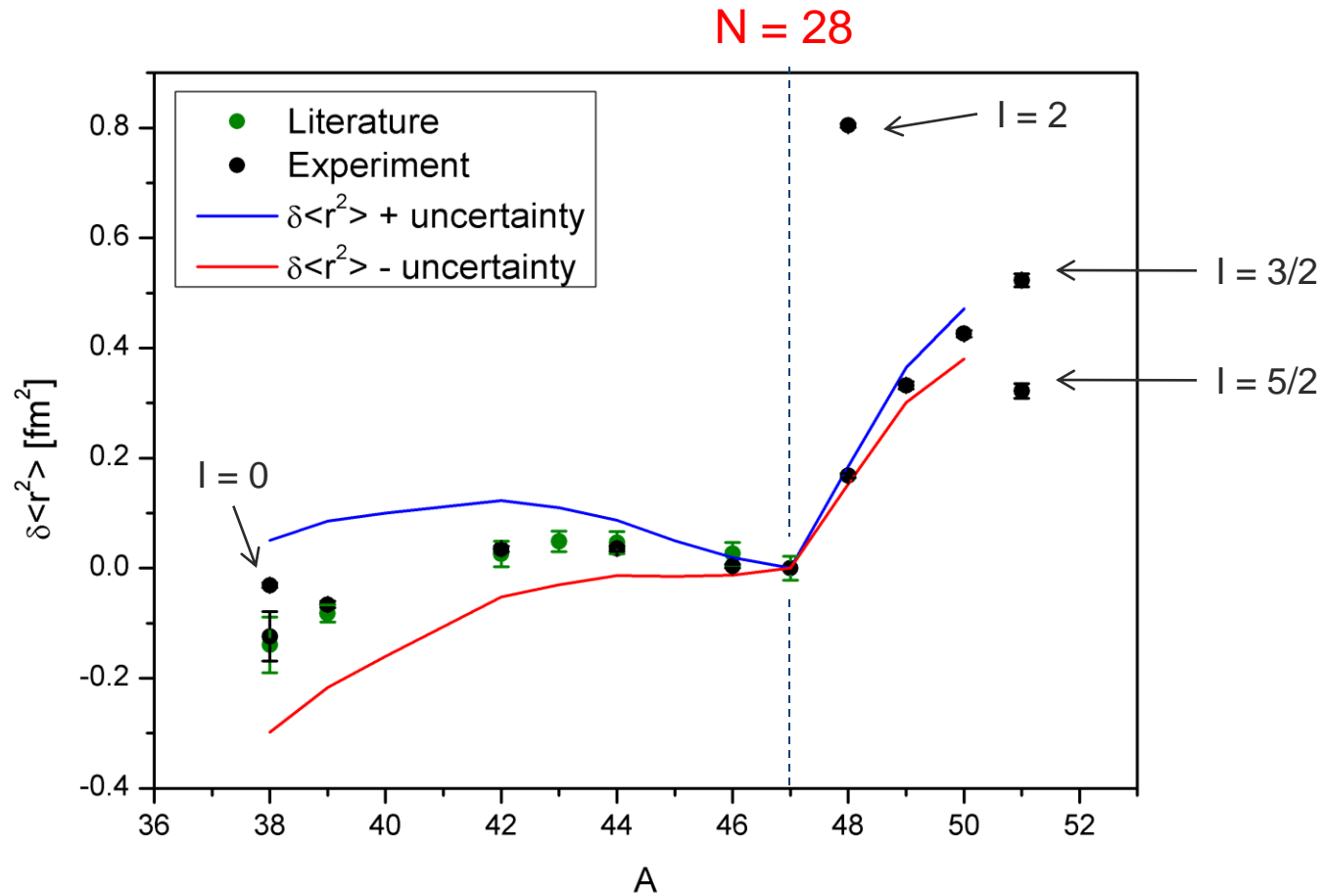
[31] J. T. Eisinger, B. Bederson, and B. T. Feld, Phys. Rev. **86**, 73 (1952).

Isotope	I^π	SDPF-NR		SDPF-U	
		configuration ($\pi \otimes \nu$)	[%]	configuration ($\pi \otimes \nu$)	[%]
^{48}K	1^-	$1d_{3/2}^{-1} \otimes 2p_{3/2}$	38	$1d_{3/2}^{-1} \otimes 2p_{3/2}$	51
		$2s_{1/2}^{-1} \otimes 2p_{3/2}$	16	$2s_{1/2}^{-1} \otimes 2p_{3/2}$	14
		$1d_{3/2}^{-1} \otimes 1f_{7/2}^{-1} 2p_{3/2}^2$	14	$1d_{3/2}^{-1} \otimes 1f_{7/2}^{-1} 2p_{3/2}^2$	11
		$1d_{3/2}^{-1} \otimes 1f_{7/2}^6 2p_{3/2}^{-1}$	5	$1d_{3/2}^{-1} \otimes 1f_{7/2}^8 2p_{1/2}$	3
		$2s_{1/2}^{-1} \otimes 1f_{7/2}^{-1} 2p_{3/2}^2$	4	$2s_{1/2}^{-1} \otimes 1f_{7/2}^{-1} 2p_{3/2}^2$	3
^{50}K	0^-	$1d_{3/2}^{-1} \otimes 2p_{3/2}^{-1}$	63	$1d_{3/2}^{-1} \otimes 2p_{3/2}^{-1}$	75
		$2s_{1/2}^{-1} \otimes 2p_{3/2}^2 2p_{1/2}$	7	$1d_{3/2}^{-1} \otimes 2p_{3/2}^2 2p_{1/2}$	4
		$1d_{3/2}^{-1} \otimes 1f_{7/2}^{-1} 2p_{3/2}^{-1} 2p_{1/2}$	6	$2s_{1/2}^{-1} \otimes 2p_{3/2}^2 2p_{1/2}$	4
		$1d_{3/2}^{-1} \otimes 2p_{3/2}^2 2p_{1/2}$	5	$1d_{3/2}^{-1} \otimes 1f_{7/2}^6 2p_{3/2}^{-1}$	3
		$1d_{3/2}^{-1} \otimes 1f_{7/2}^6 2p_{3/2}^{-1} 1f_{5/2}^2$	4	$1d_{3/2}^{-1} \otimes 1f_{7/2}^{-1} 2p_{3/2}^{-1} 2p_{1/2}$	2

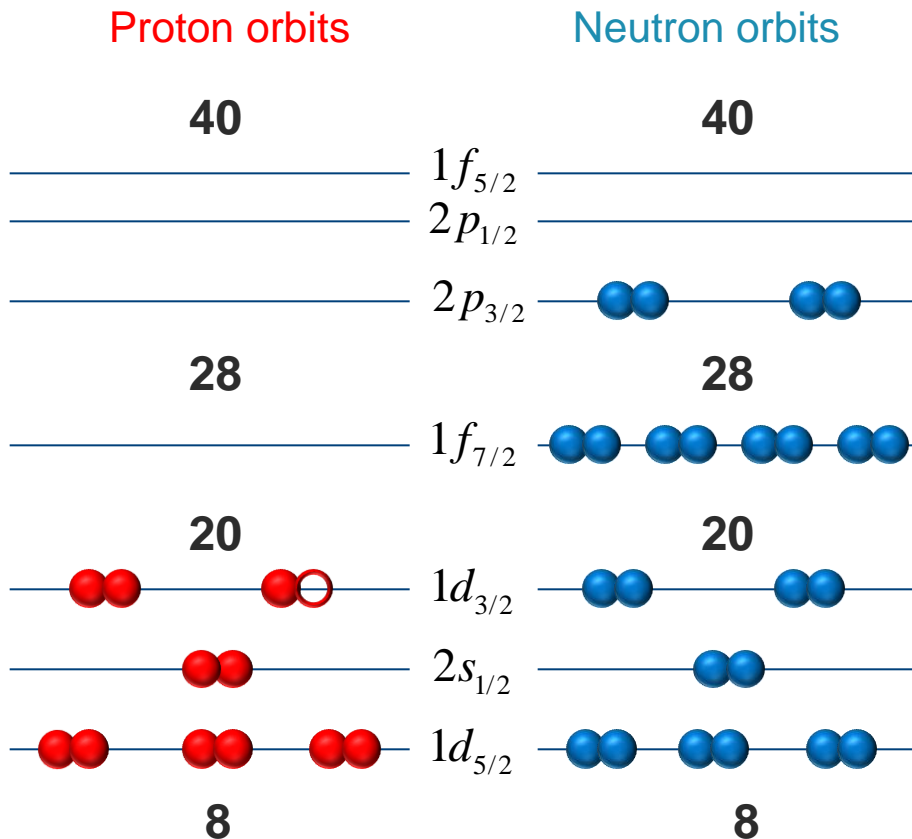
Composition of the wave function



Charge radii



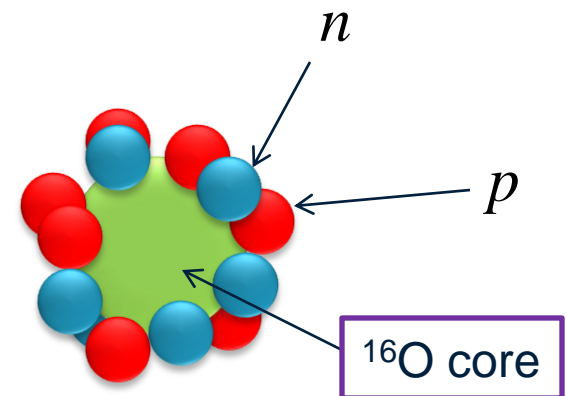
Theoretical model



Effective interactions:

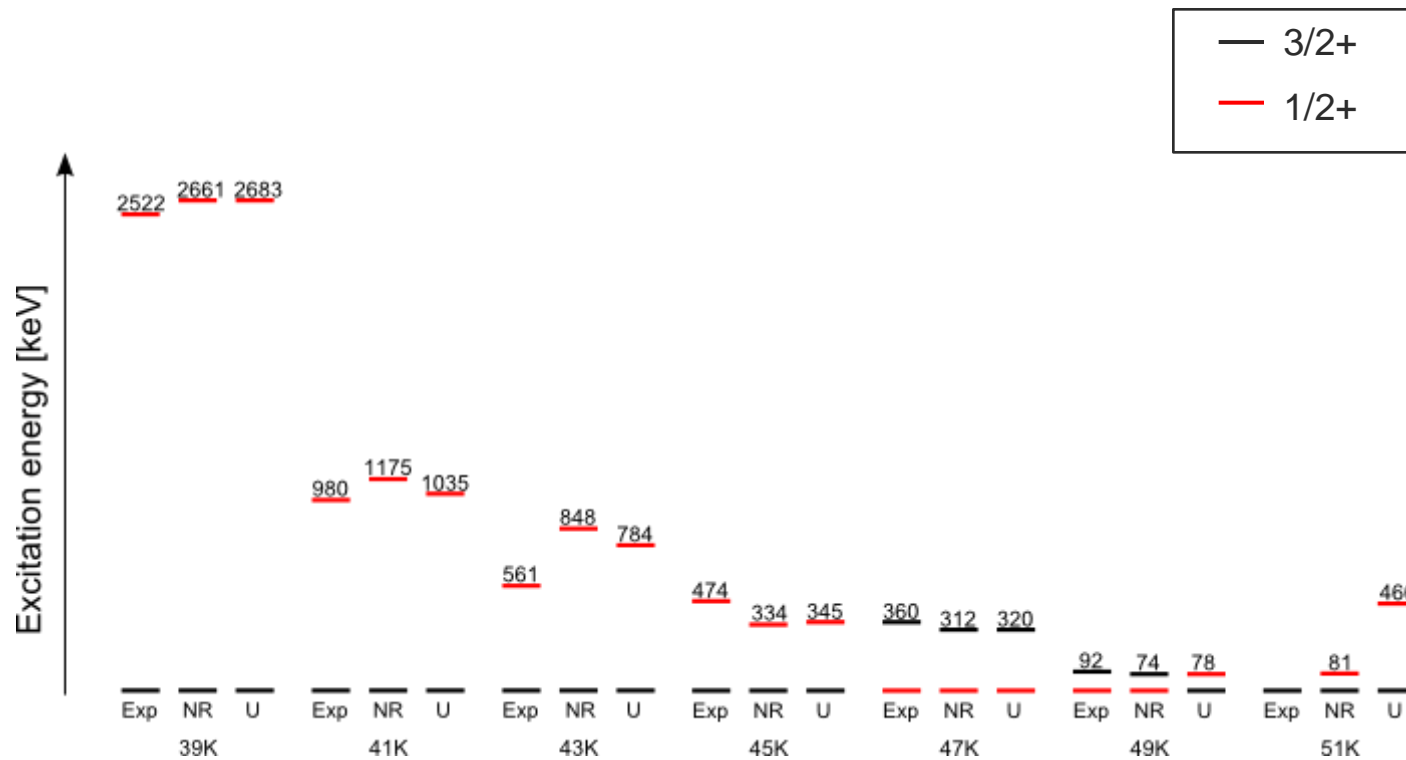
SDPF-NR¹

SDPF-U²



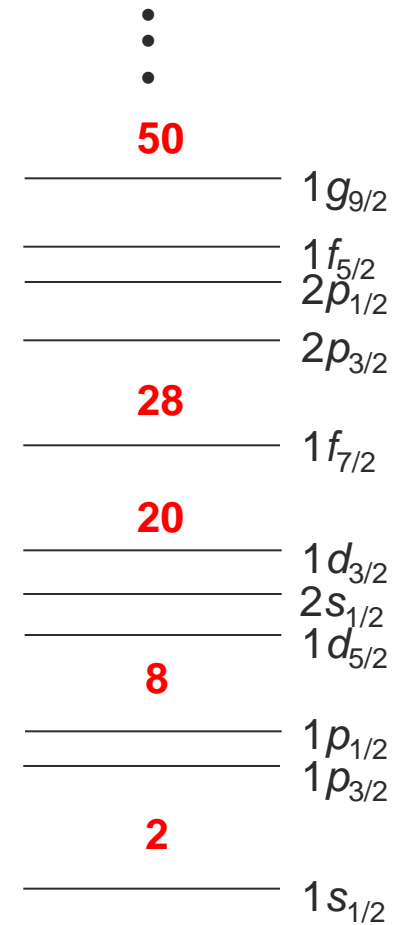
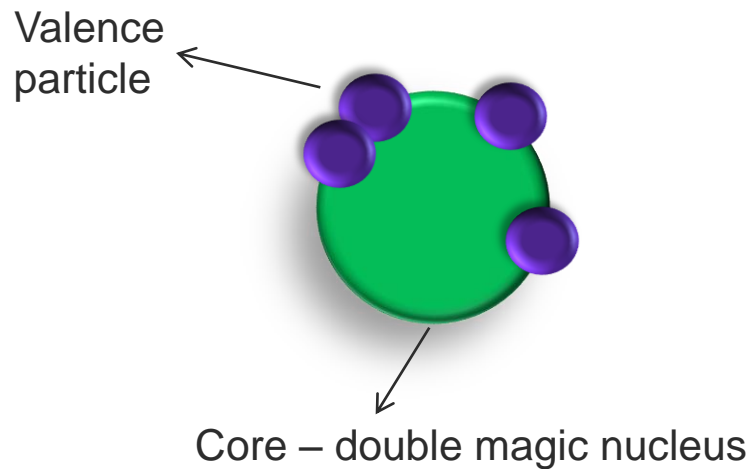
¹ J. Retamosa *et al.*, Phys. Rev. C 55, 1266 (1997)
S. Nummela *et al.*, Phys. Rev. C 64, 054313 (2001)

² F. Nowacki and A. Poves, Phys. Rev. C 79, 014310 (2009): ³⁵Si (Z = 14), ⁴⁷Ar (Z = 18) and ⁴¹Ca (Z = 20)



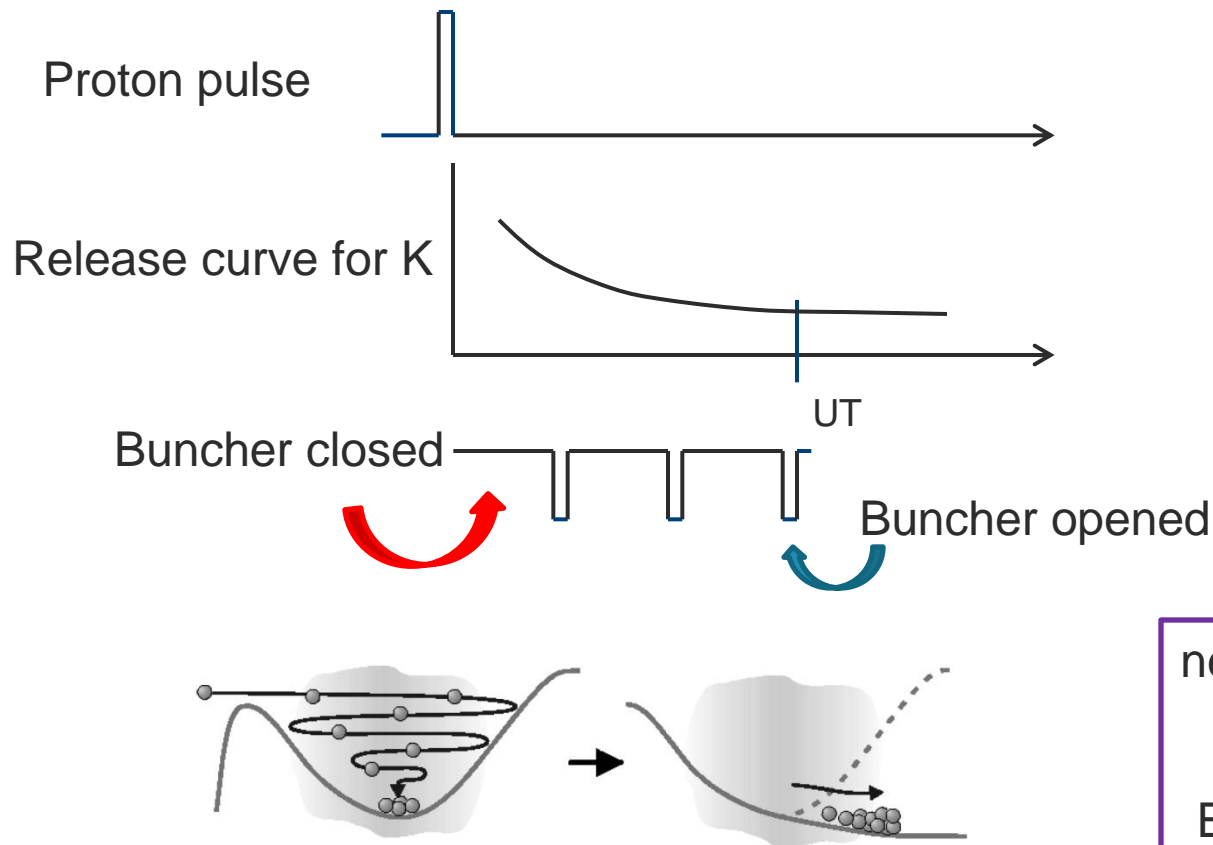
Motivation

- Shell model:
 - Orbits (n/l) with max. $2j+1$ particles
 - Shell gaps
 - Magic numbers



- “Exotic” nuclei (large N/Z): shell evolution

Collinear Laser Spectroscopy



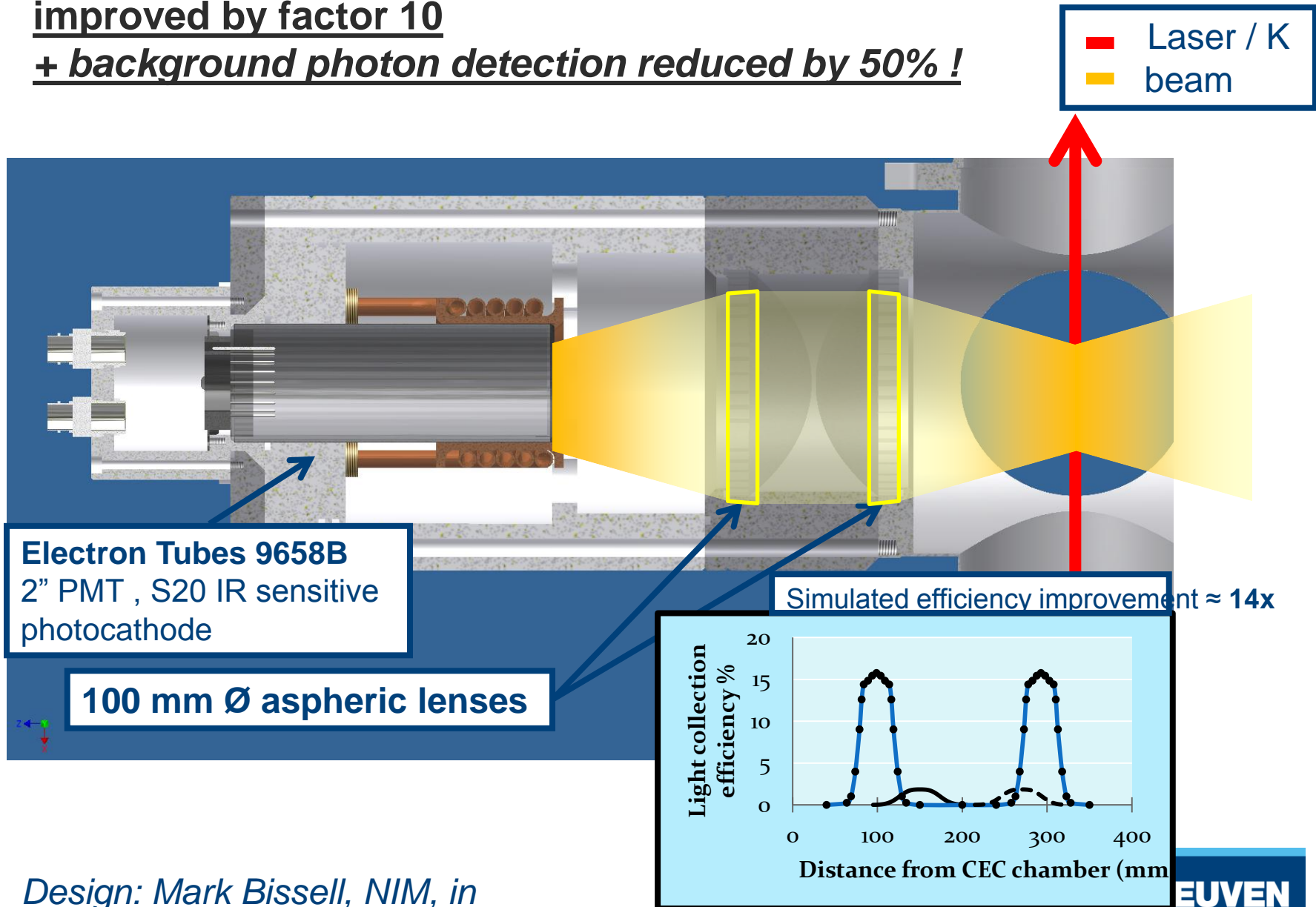
- Accumulation Time (AT): 90 ms
- Release Time (RT): 6 μ s
- Useful Time (UT): $3 \cdot AT$

new lens geometry + 4 PMTs

↓

Efficiency: 10 times improved

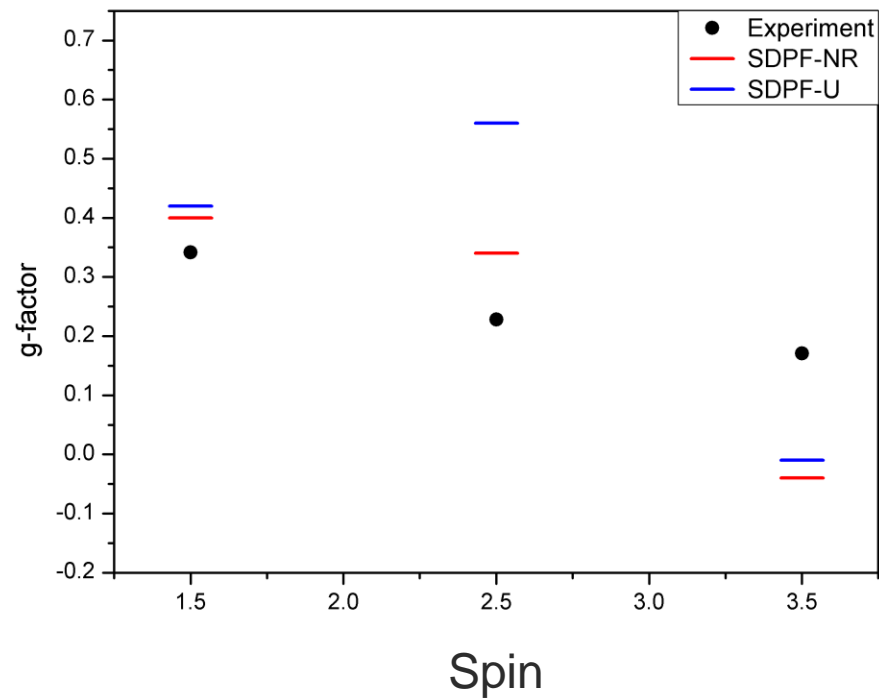
Optical detection efficiency for K (red light)
improved by factor 10
+ background photon detection reduced by 50% !



Design: Mark Bissell, NIM, in preparation

Spin	g_{exp}	SDPF-NR	SDPF-U
3/2	0.3419(15)	0.40 [E = 0]	0.42 [E = 0]
5/2	0.2279(11)	0.34 [E = 1725]	0.56 [E = 2018]
7/2	0.1710(8)	-0.04 [E = 1793]	-0.01 [E = 2040]

E in keV



References:

- ^{39}K : A. Beckmann *et al.*, Z. Physics, Volume 270 (1974) 173-186
- Radii: A-M Martensson-Pendrill *et al.*, J. Phys. B: At. Mol.opt.Phys. 23(1990)

Energy levels:

- ^{43}K : Measday *et al.*, PRC 73, 045501 (2006)
- ^{45}K : Huck *et al.*, PRC 21, 2 (1980)
- ^{47}K : Weissman *et al.*, PRC 70, 024304 (2004)
- ^{49}K : Broda *et al.*, PRC 82, 034319 (2010)
- ^{51}K : Perrot *et al.*, PRC 74, 014313 (2006)